

# Data Visualization (CSCI 627/490)

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## Isosurfacing & Volume Rendering

Dr. David Koop

# Data Wrangling

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- Problem 1: Visualizations need data
- Solution: The Web!
- Problem 2: Data has extra information I don't need
- Solution: Filter it
- Problem 3: Data is dirty
- Solution: Clean it up
- Problem 4: Data isn't in the same place
- Solution: Combine data from different sources
- Problem 5: Data isn't structured correctly
- Solution: Reorder, map, and nest it

# JavaScript Data Wrangling Resources

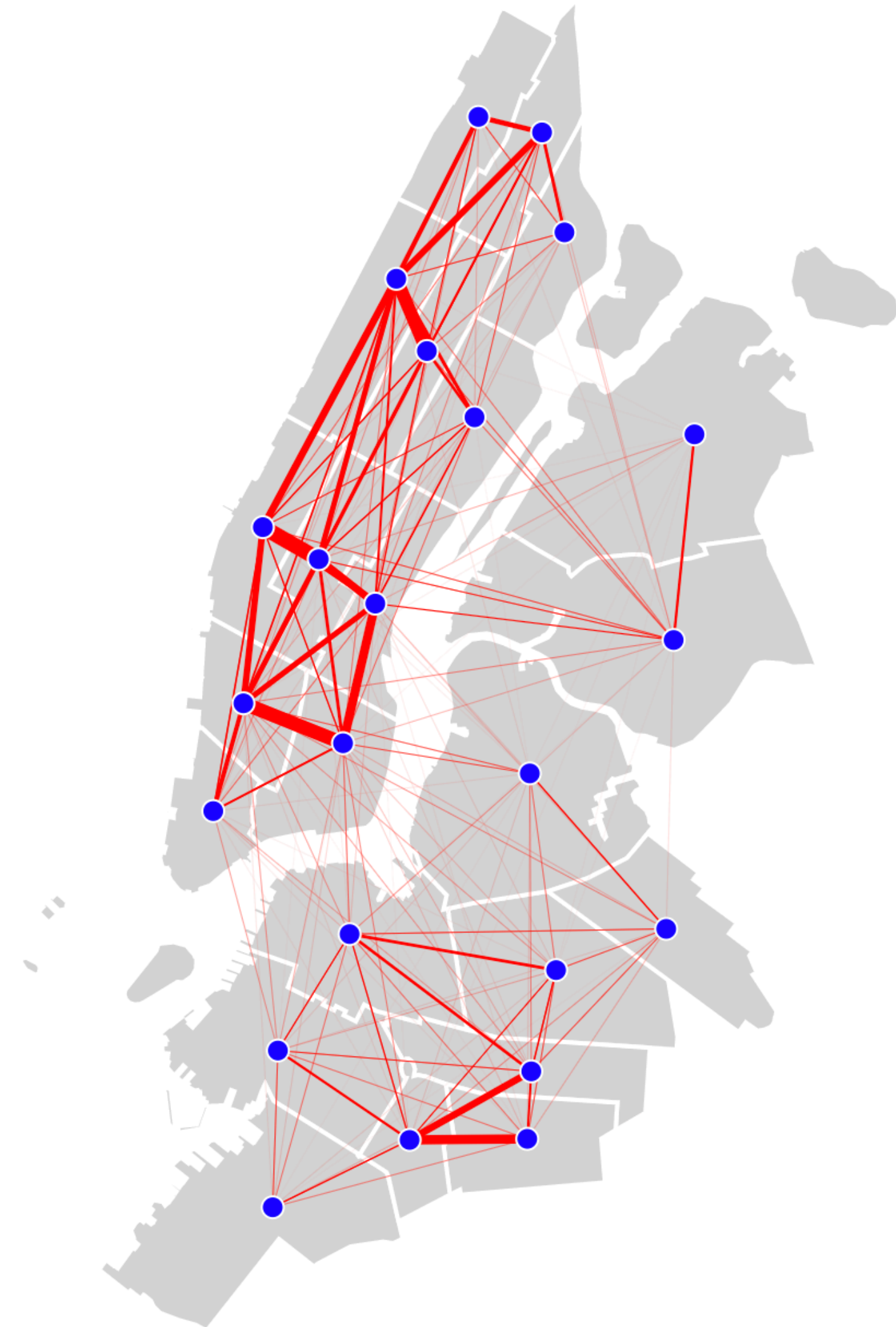
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- Latest version: <https://observablehq.com/@berkeleyvis/learn-js-data>
- My old version: <https://observablehq.com/@dakoop/learn-js-data>
- Based on <http://learnjsdata.com/>
- Good coverage of data wrangling using JavaScript

# Assignment 5

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- Map of Citi Bike trips
  - Multiple Views
  - Linked Highlighting
  - Filtering
  - Aggregation
- Due Monday, Nov. 23



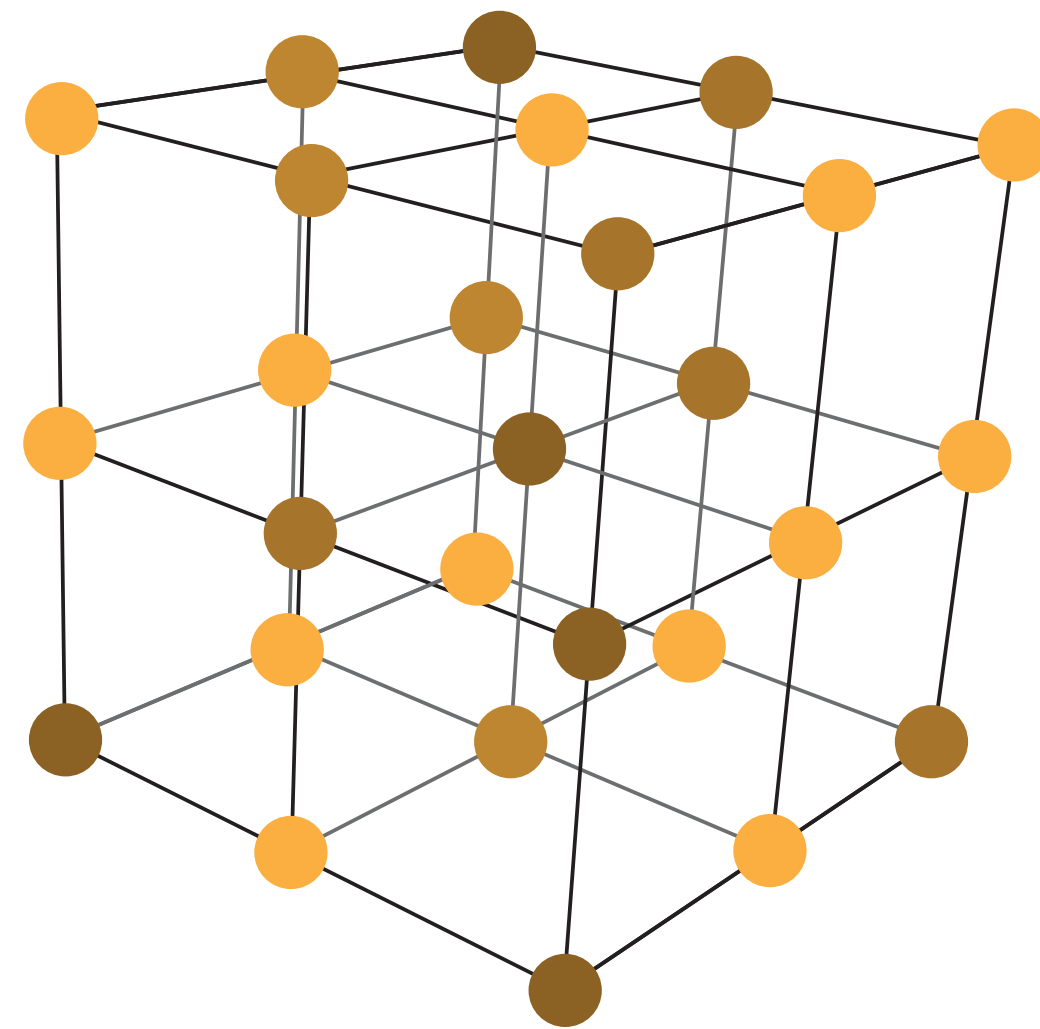
# Projects

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- Keep working on implementation
- Be creative, don't copy
- Think about interaction
- Presentations on the last day of class (Dec. 3)
  - Plan to use Blackboard
  - Upload to Blackboard beforehand in case of technical issues

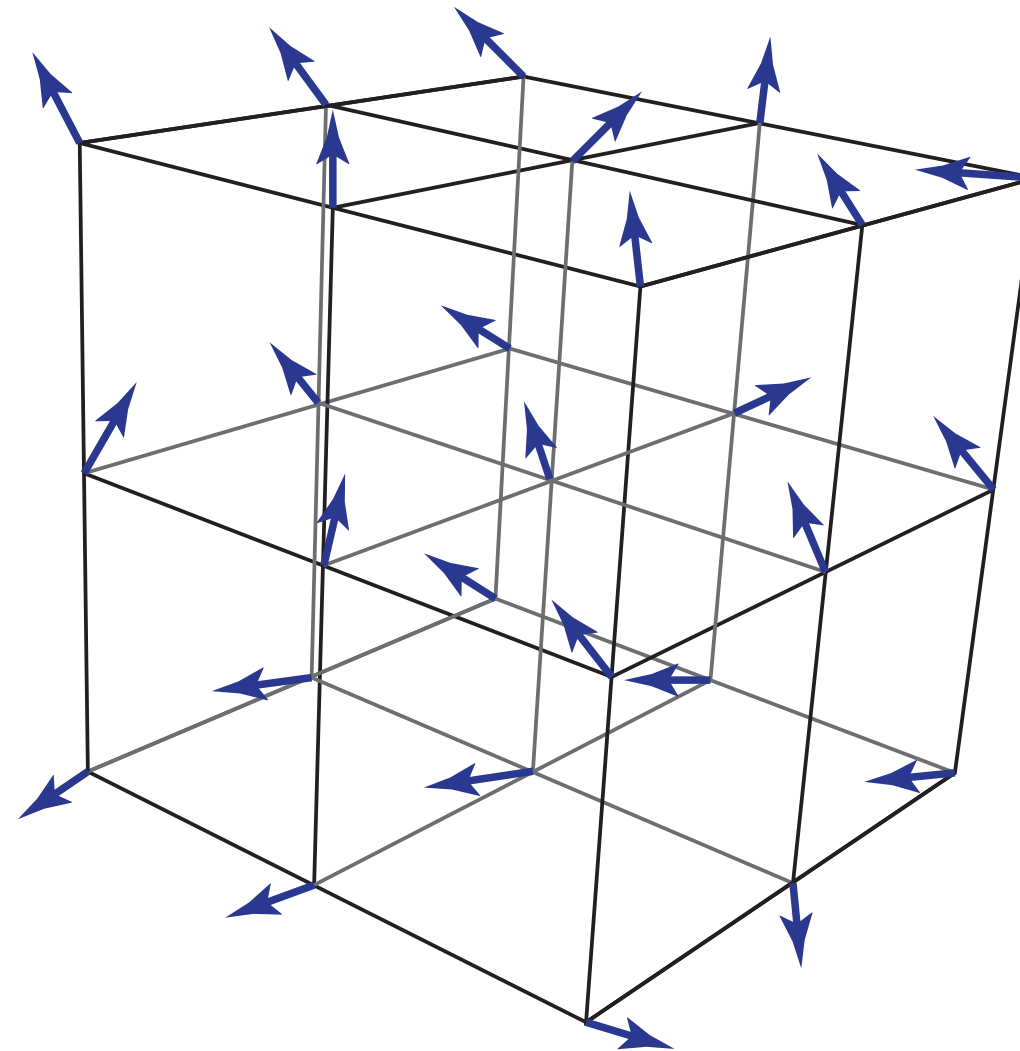
# Course Evaluations

# Fields in Visualization



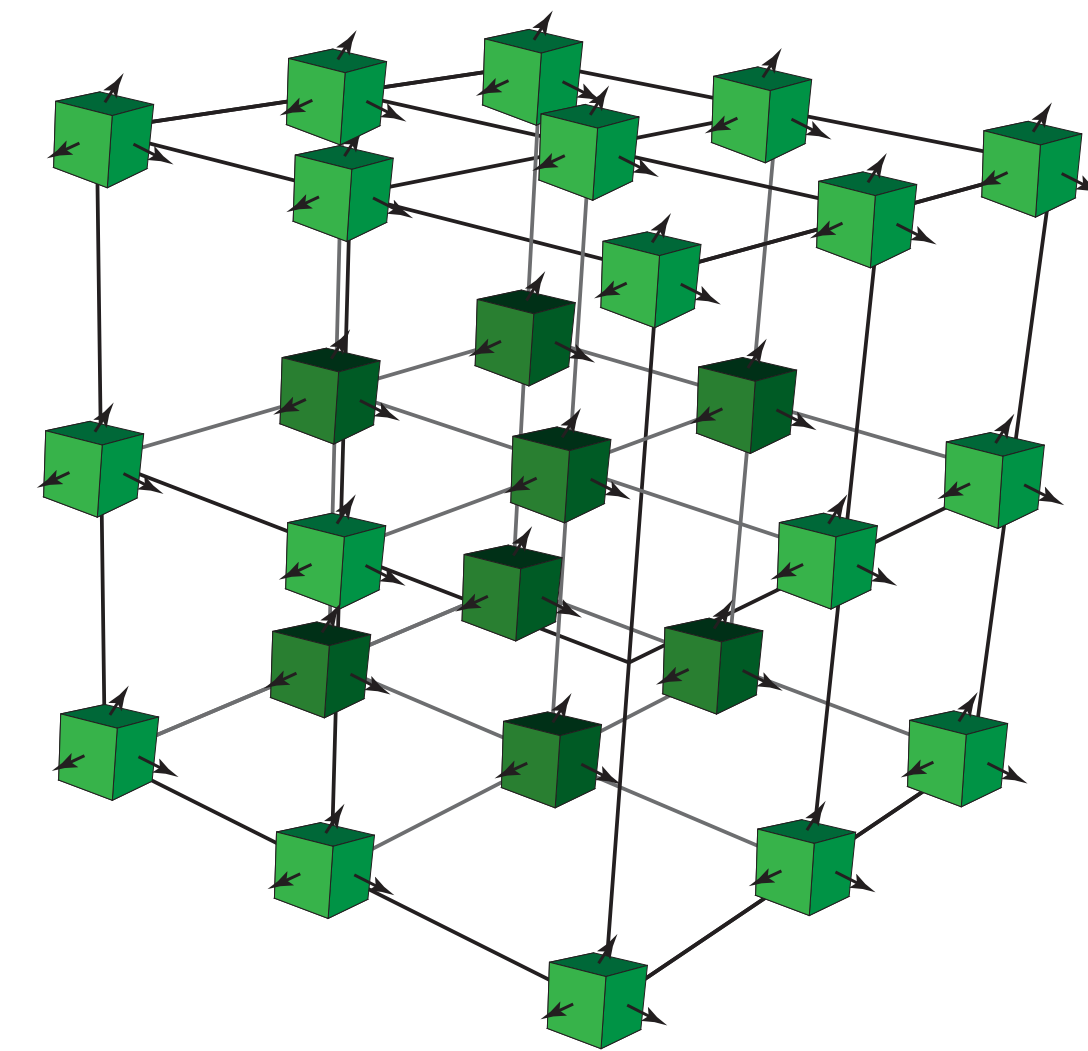
Scalar Fields

(Order-0 Tensor Fields)



Vector Fields

(Order-1 Tensor Fields)



Tensor Fields

(Order-2+)

Each point in space has an associated...

$s_0$

Scalar

$$\begin{bmatrix} v_0 \\ v_1 \\ v_2 \end{bmatrix}$$

Vector

$$\begin{bmatrix} \sigma_{00} & \sigma_{01} & \sigma_{02} \\ \sigma_{10} & \sigma_{11} & \sigma_{12} \\ \sigma_{20} & \sigma_{21} & \sigma_{22} \end{bmatrix}$$

Tensor



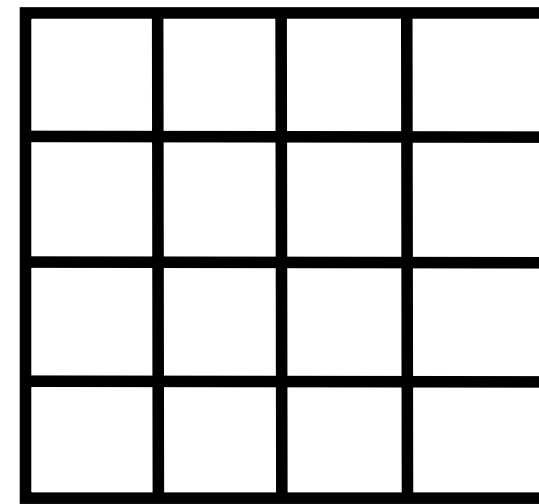
# Grids

- [illegible]

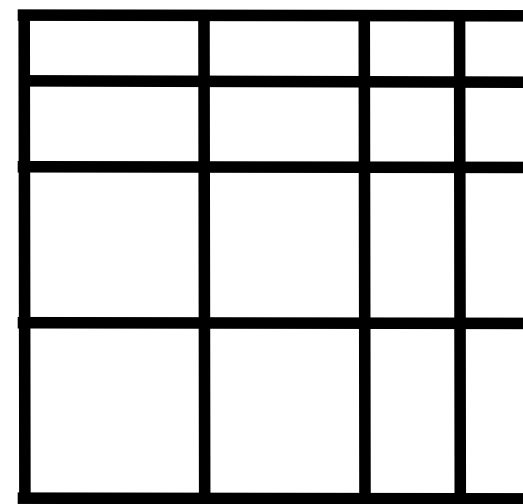


# Grids

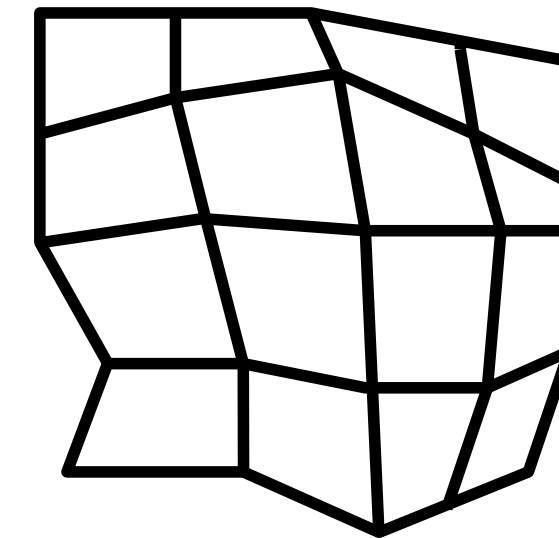
- Remember we have continuous data and want to sample it in order to understand the **entire** domain
- Possible schemes?



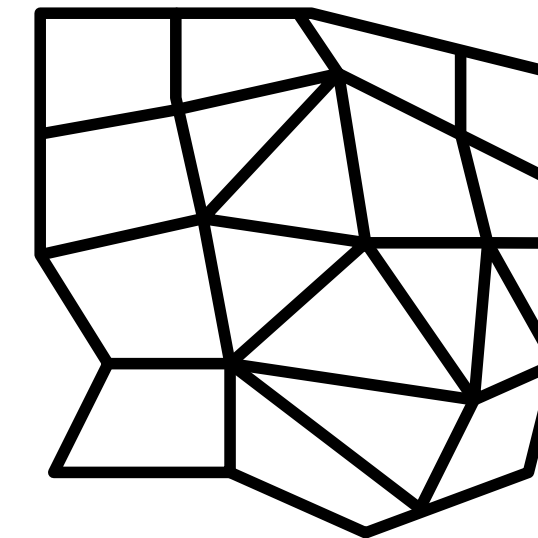
uniform



rectilinear



structured

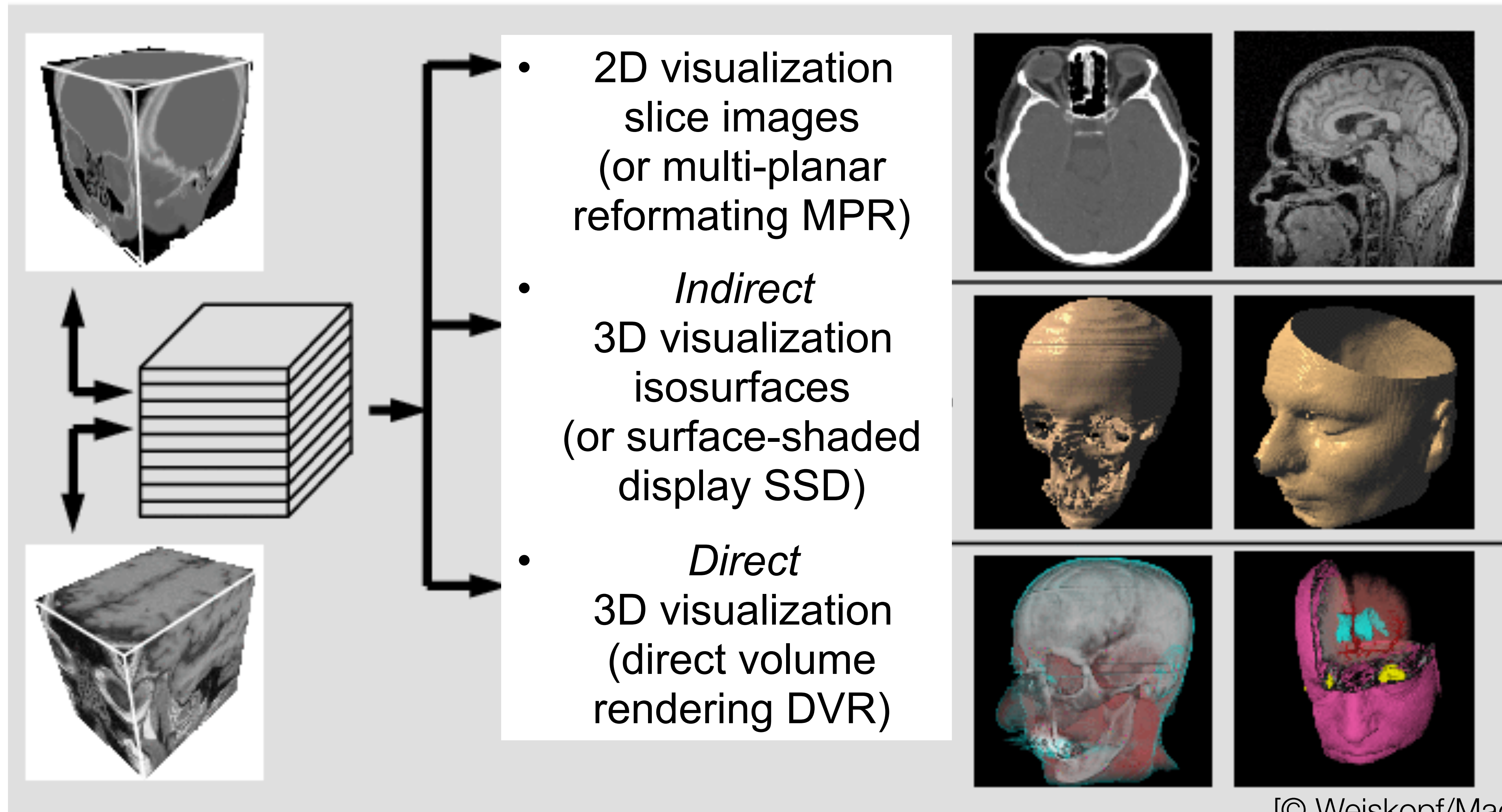


unstructured

[© Weiskopf/Machiraju/Möller]

- Geometry: the spatial positions of the data (points)
- Topology: how the points are connected (cells)
- Type of grid determines how much data needs to be stored for both geometry and topology

# Visualizing Volume (3D) Data



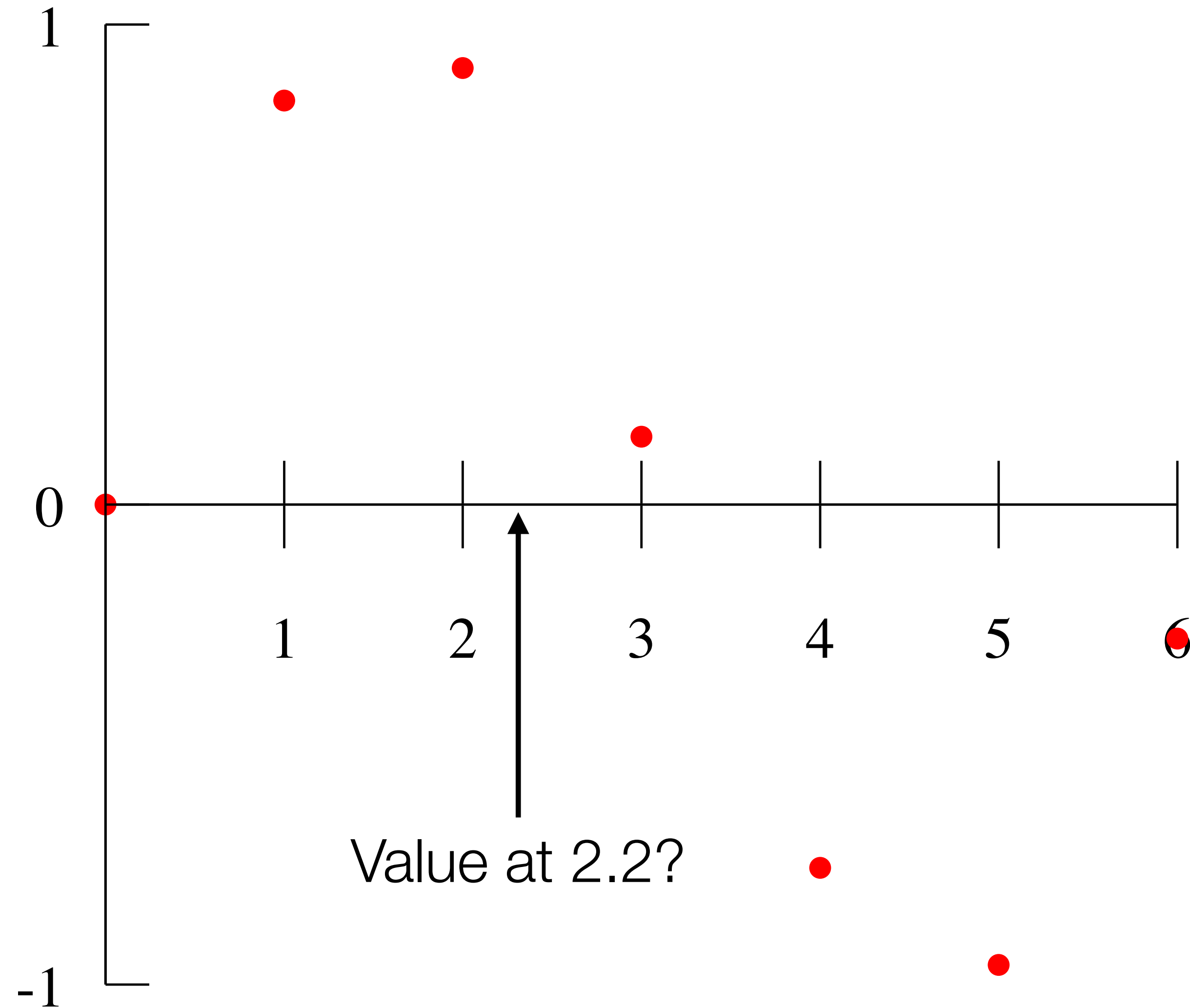
[© Weiskopf/Machiraju/Möller]

# Data

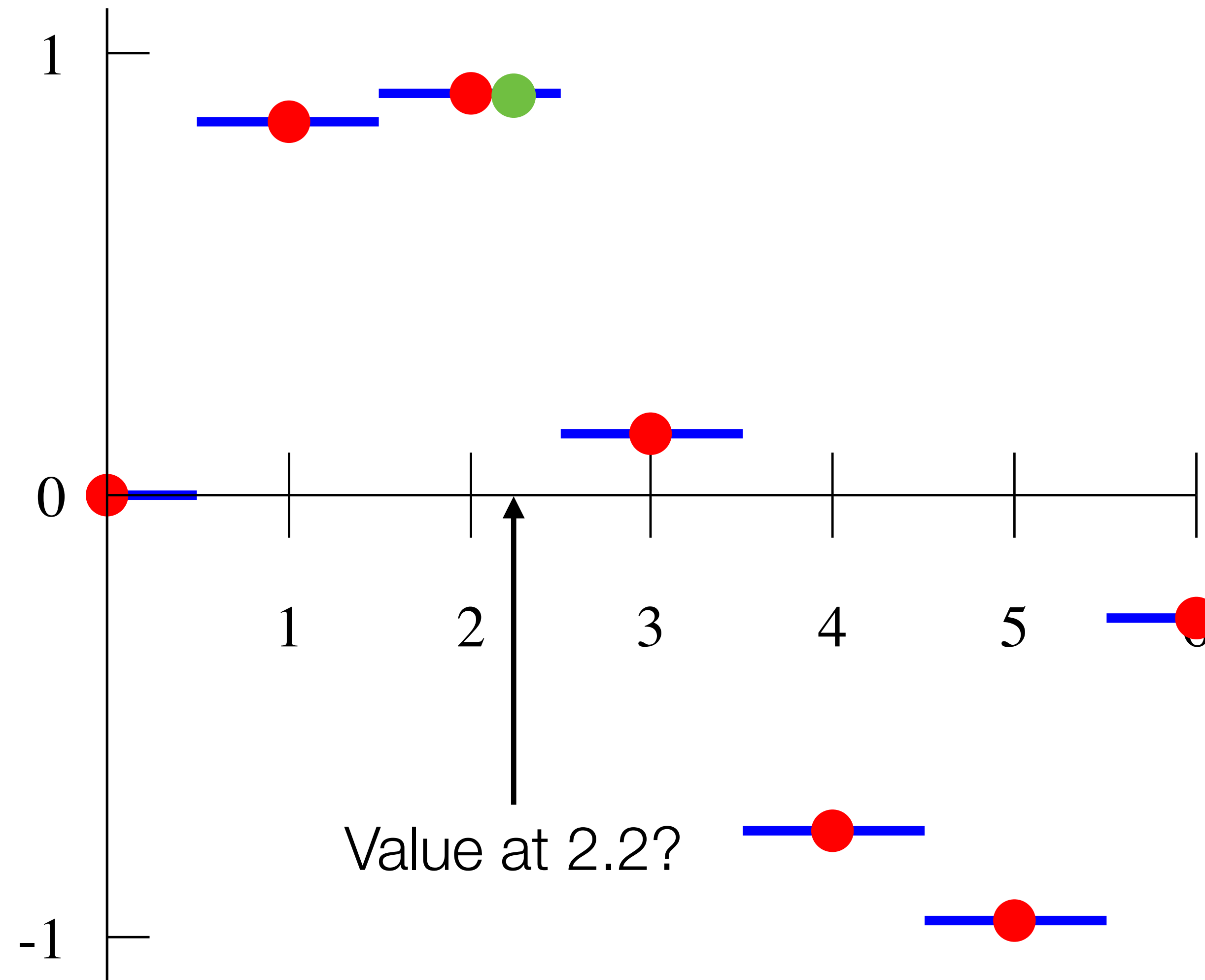
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- In this lecture, we will be considering **scalar** data: a single value at each point
- Our data is always discrete, what is the value of a point not exactly on our grid?
- Need a method to determine what these values are...

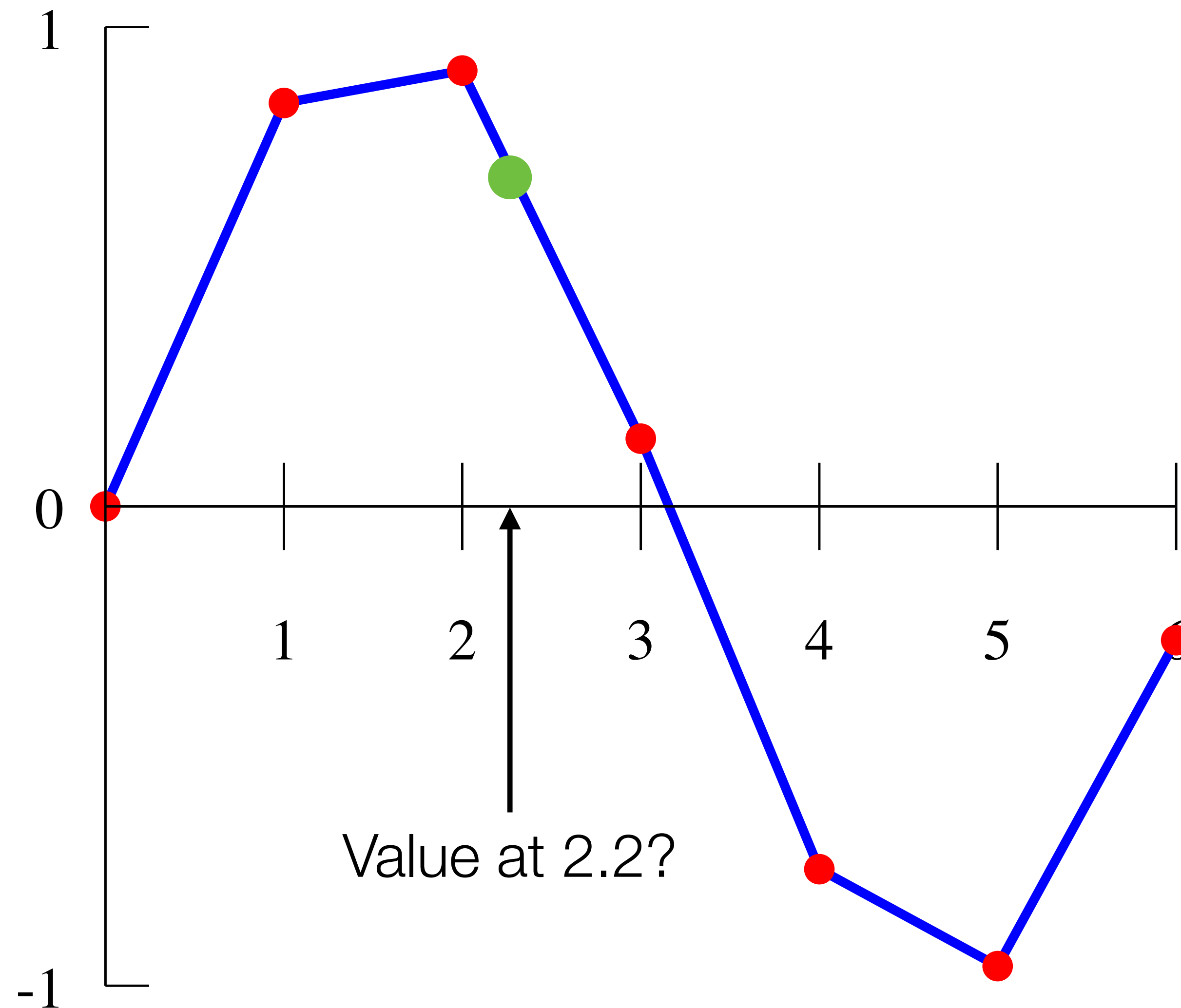
# Interpolation



# Nearest Neighbor Interpolation



# Linear Interpolation



# Interpolation

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- Other schemes:
  - polynomial interpolation
  - splines
  - more...

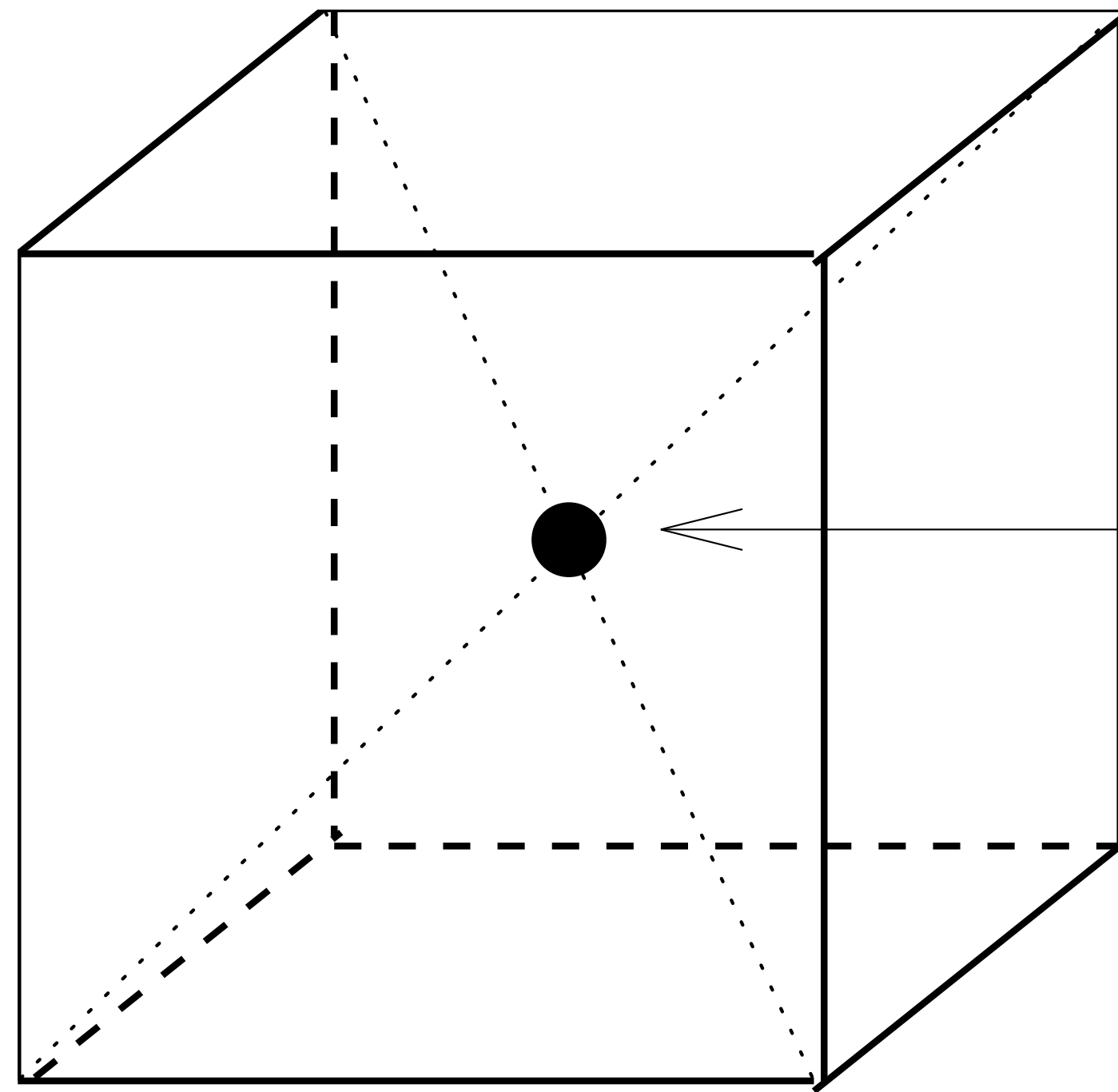


# Dimensions of Data

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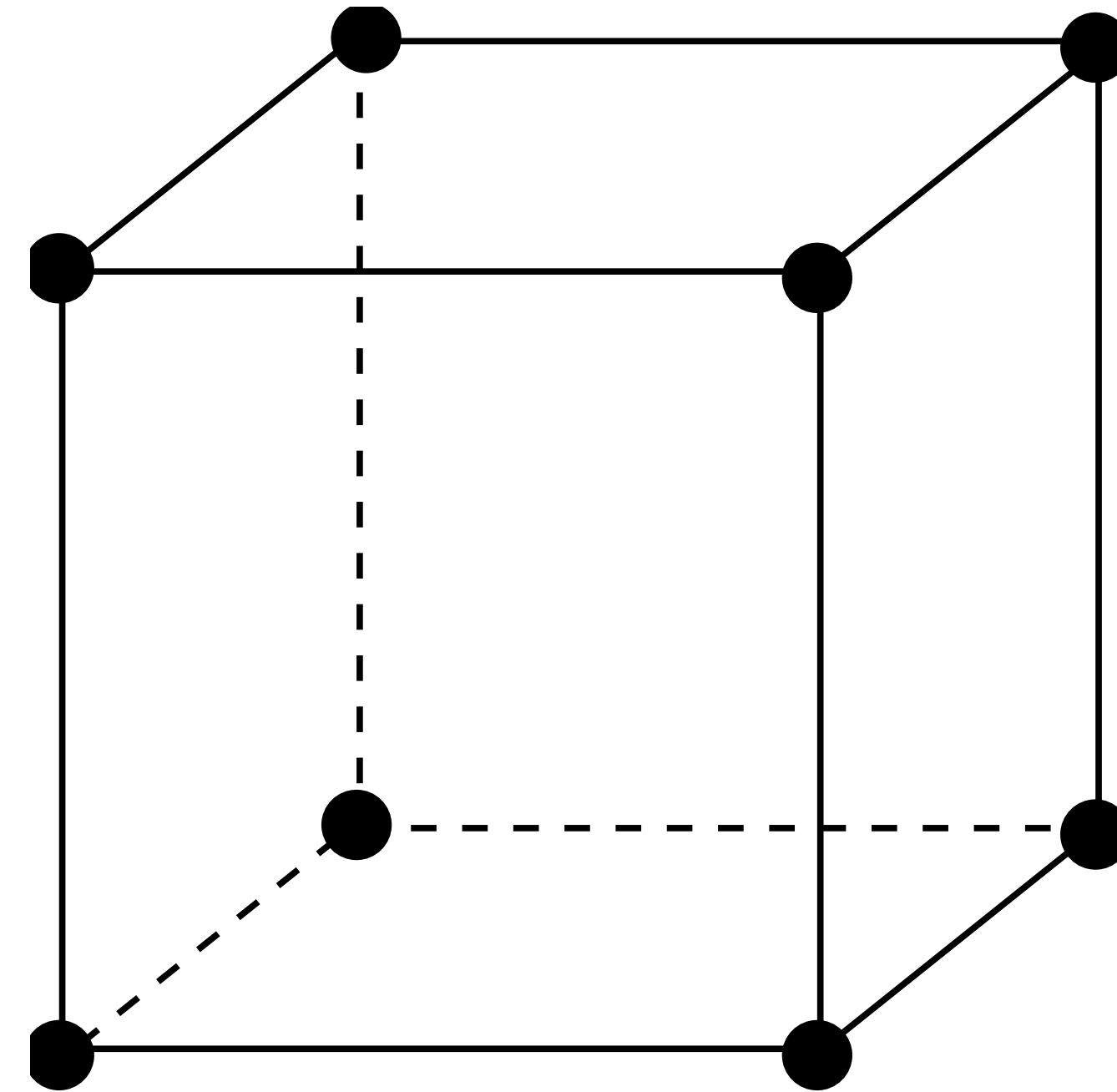
- 1-Dimension: data along a line
  - Example: temperature along my drive from Massachusetts to Illinois
- 2-Dimensional: data on a plane
  - Example: temperature on the surface of a pond
- 3-Dimensional: data in our normal world (data in a **volume**)
  - Example: temperature at every point in the room
- Complexity increases as we add dimensions
- Visualization complexity also increases
- Often, want to be able to see phenomena as we see them in real life settings

# 3D: Voxels and Cells



**VOXEL**

**gridpoint**

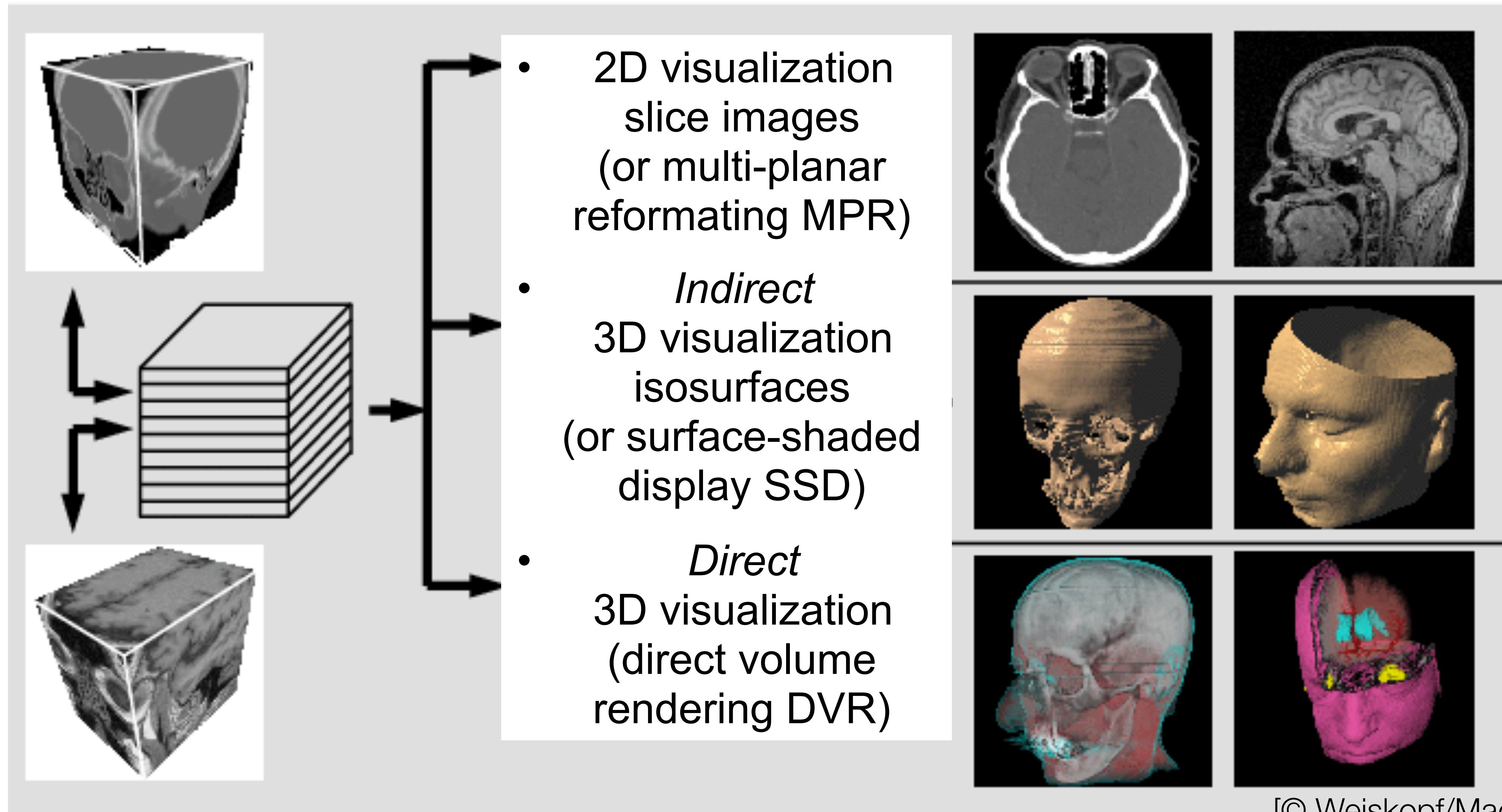


**gridpoint**

**CELL**

[from <http://www.cs.rug.nl/~michael/FANTOM/FANTOM1a.pdf>]

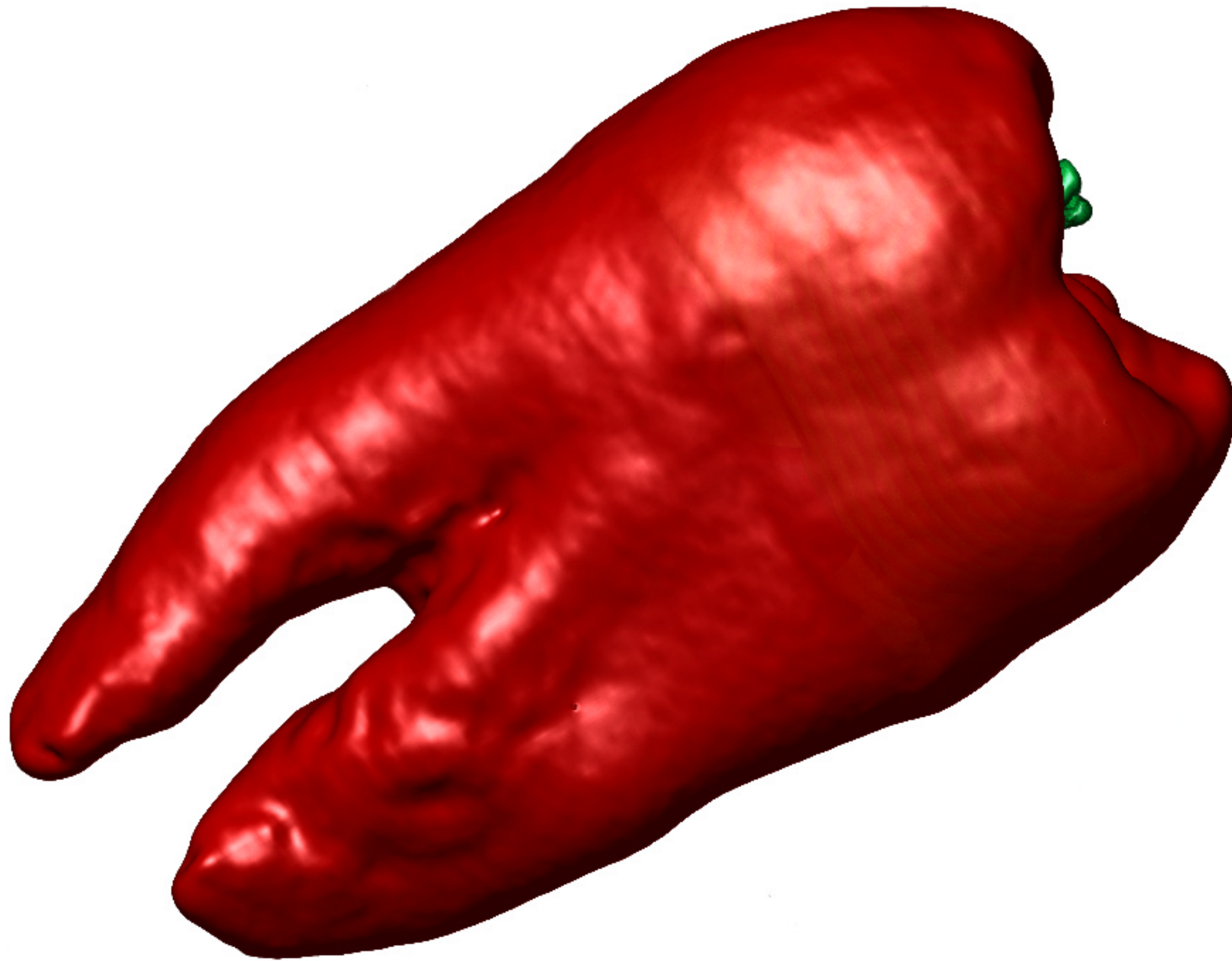
# Visualizing Volume (3D) Data



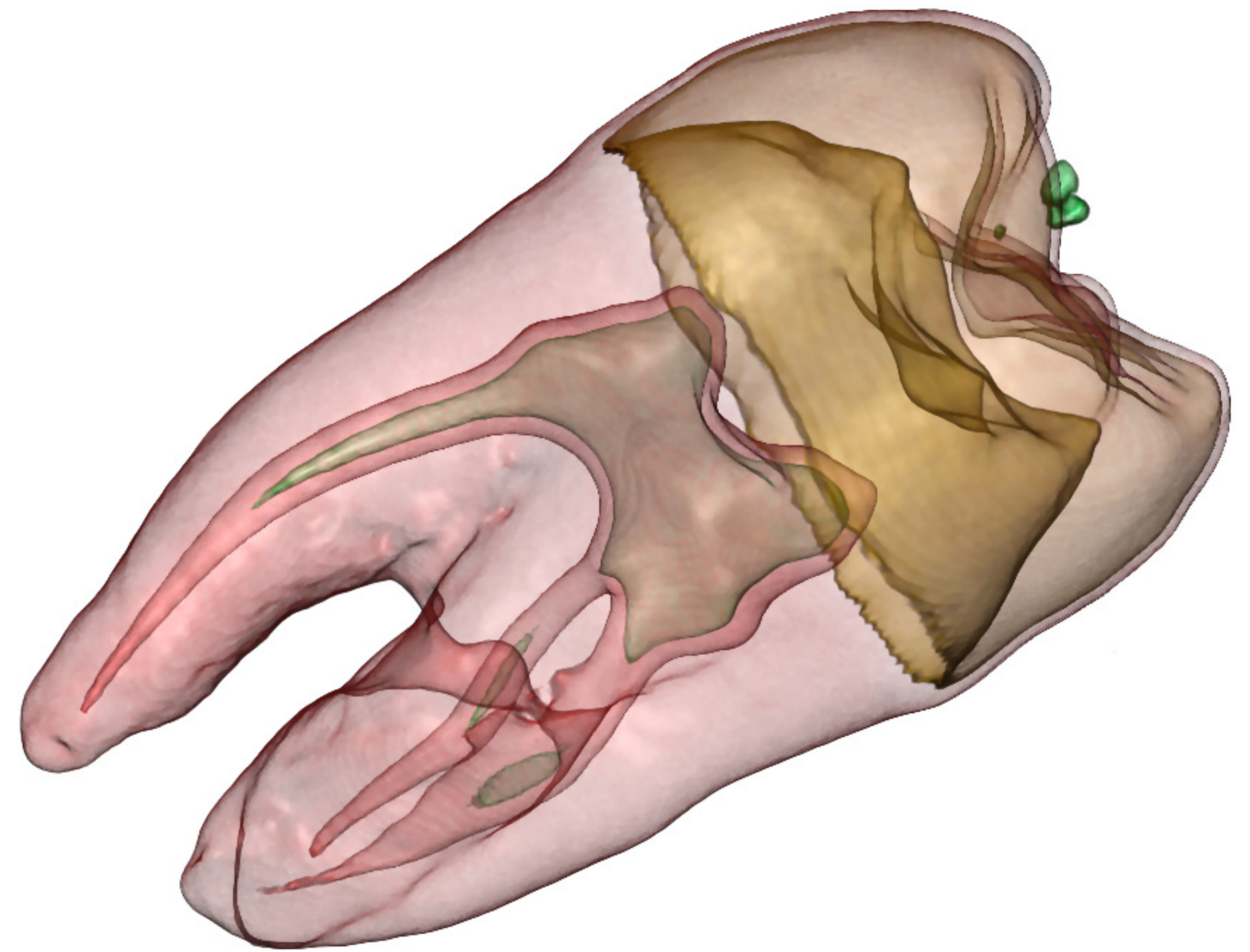
[© Weiskopf/Machiraju/Möller]



# Visualizing Volume (3D) Data



(a) An isosurfaced tooth.



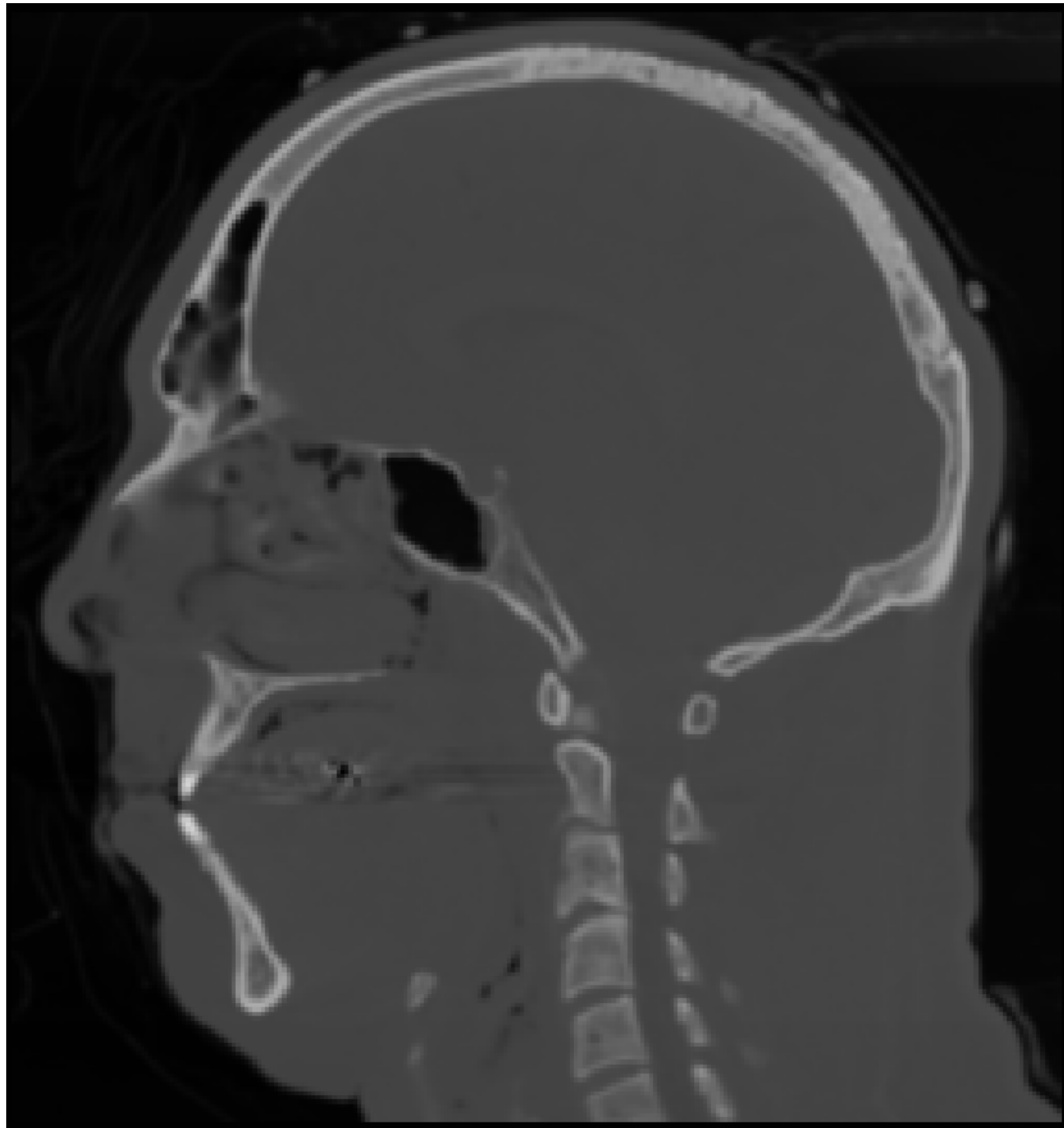
(b) Multiple isosurfaces.

[J. Kniss, 2002]

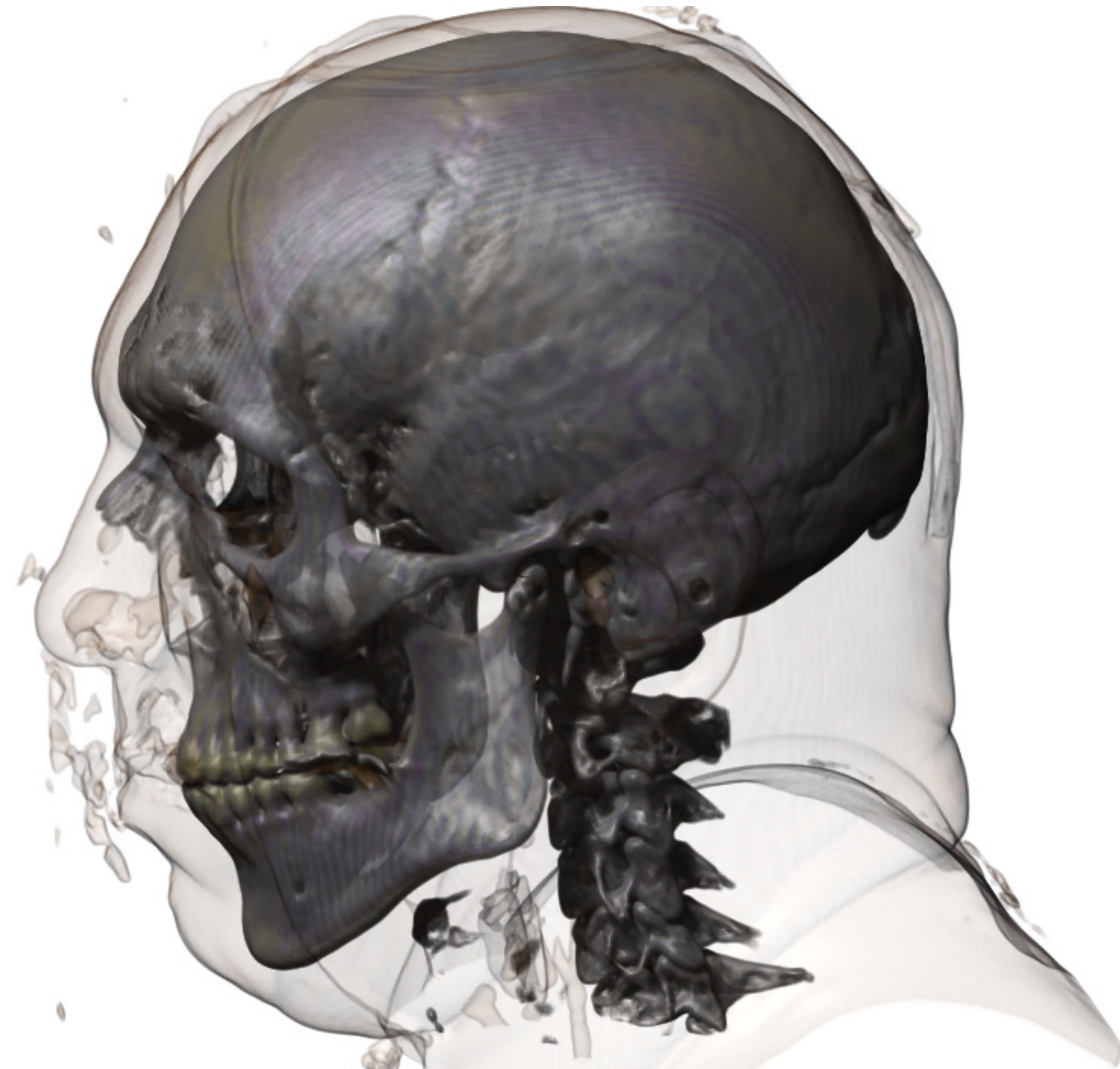


# Visualizing Volume (3D) Data

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(a) 2D slice

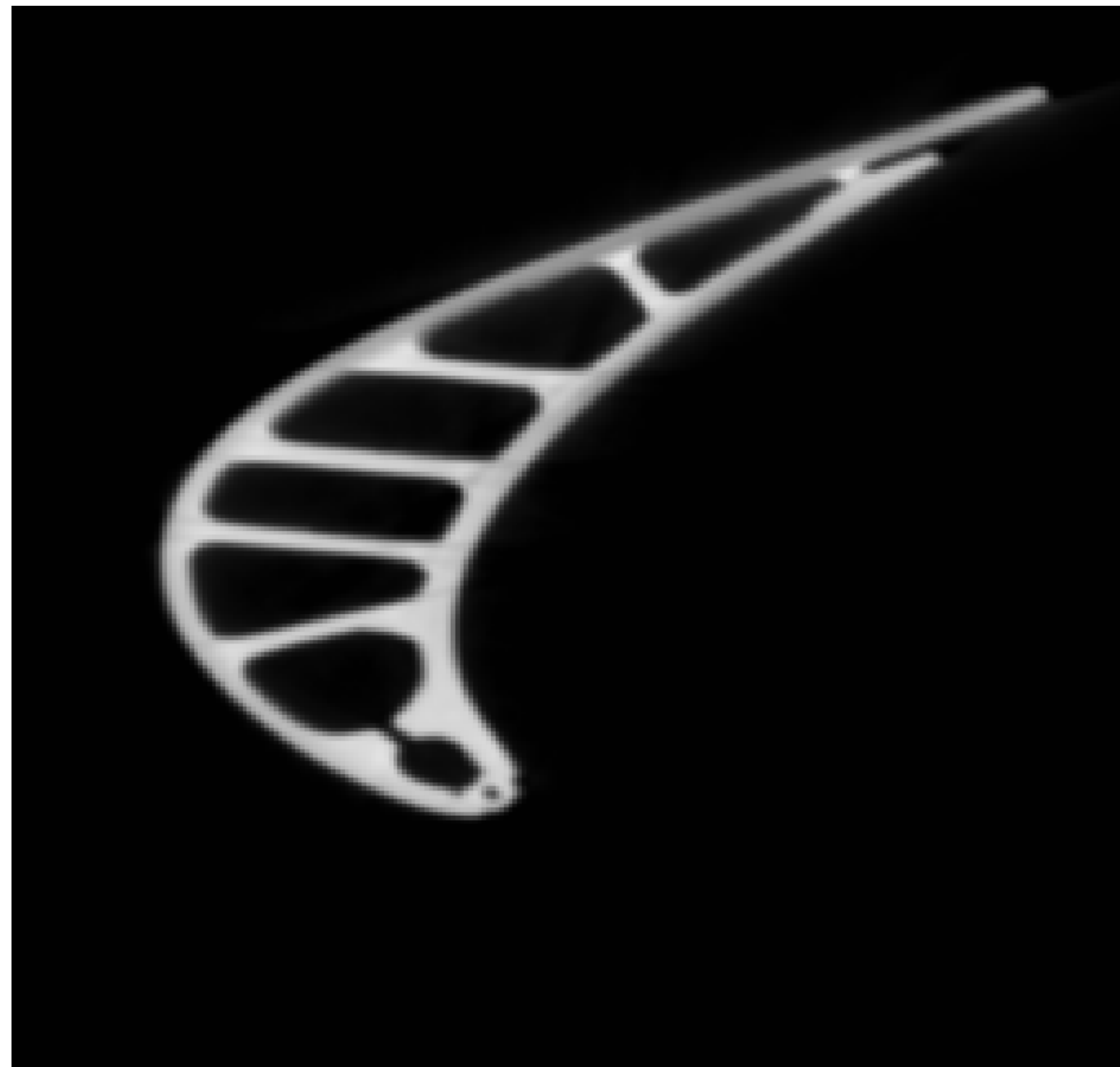


(b) Volume Rendering

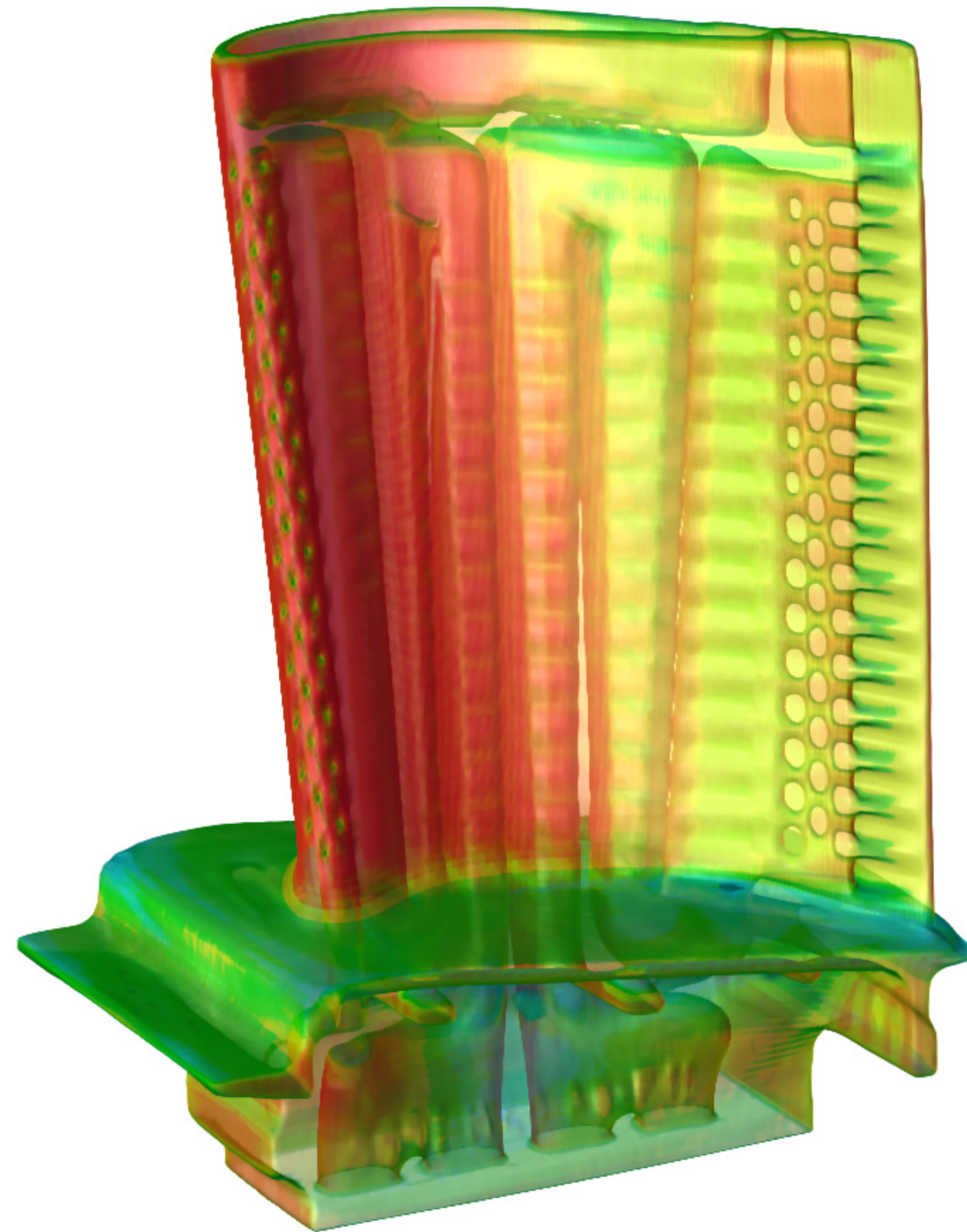
[J. Kniss, 2002]



# Visualizing Volume (3D) Data



(a) 2D slice



(b) Volume Rendering

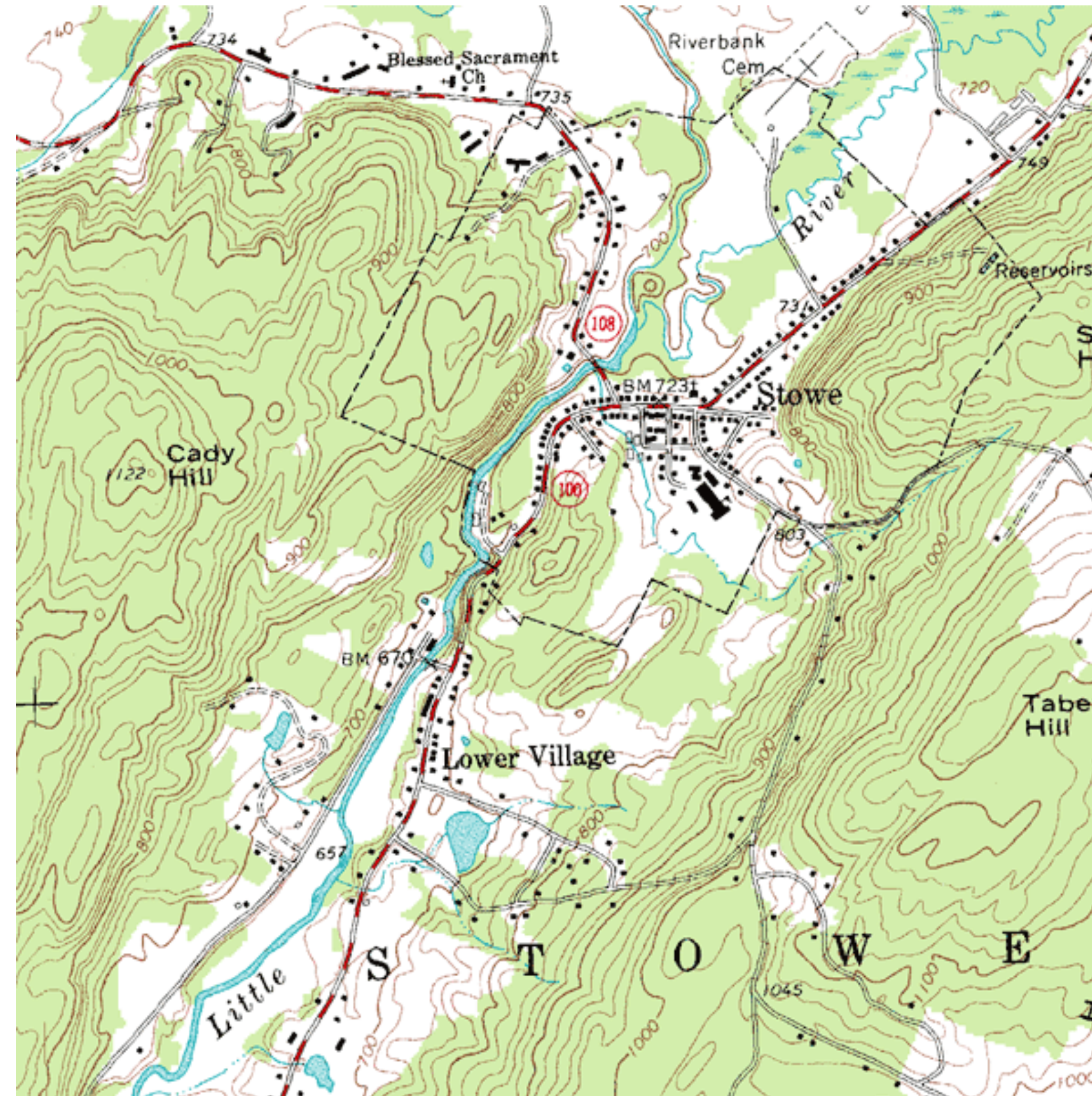
[J. Kniss, 2002]

How have we encoded 3D scalar data before?  
Hint: Think about elevation maps



# Isolines (2D)

- Isoline: a line that has the same scalar value at all locations
- Example: Topographical Map



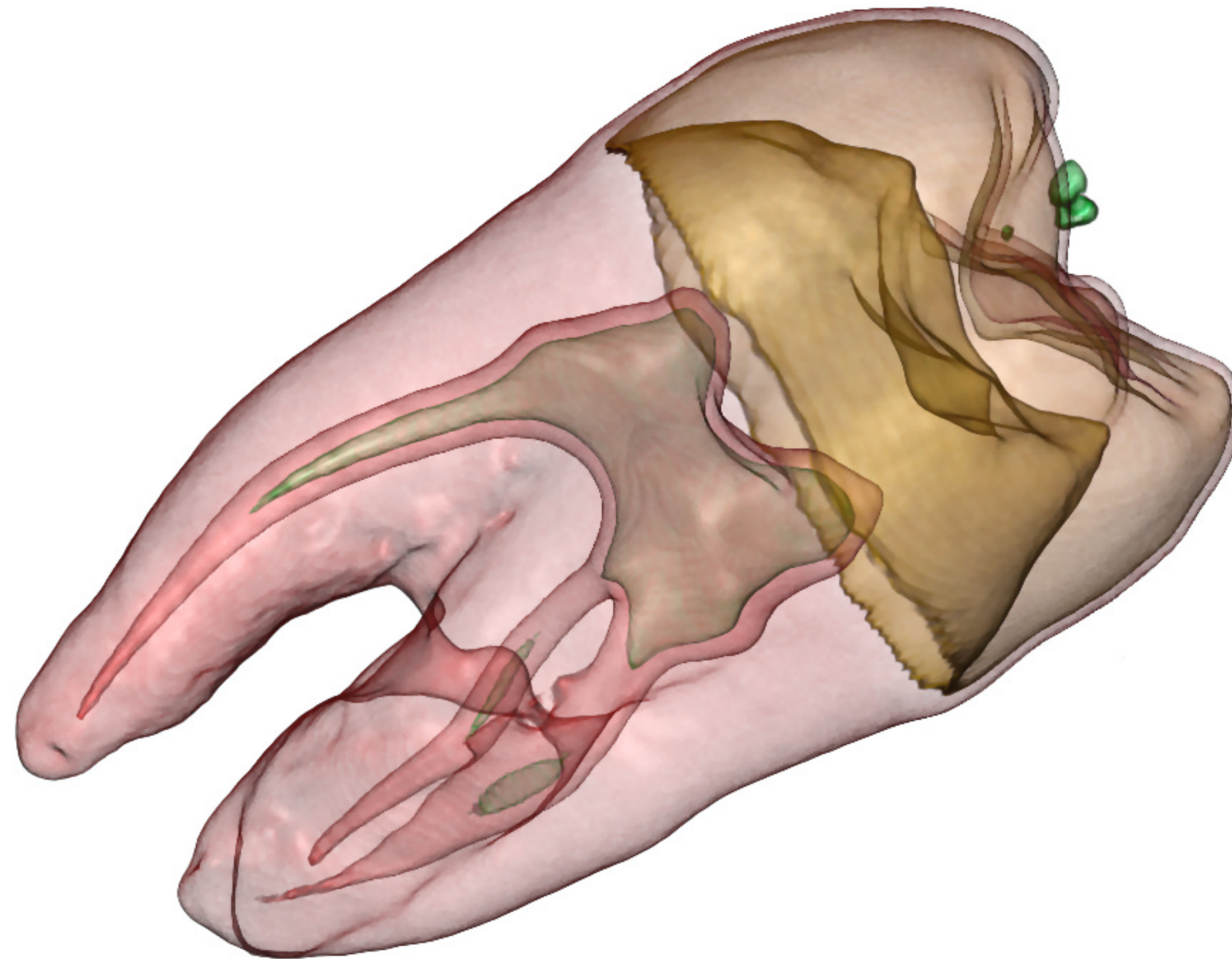
[USGS via Wikipedia]



# Isosurfaces (3D)

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- Isosurface: a surface that has the same scalar value at all locations
- Often use multiple isosurfaces to show different levels



[J. Kniss, 2002]

# How?

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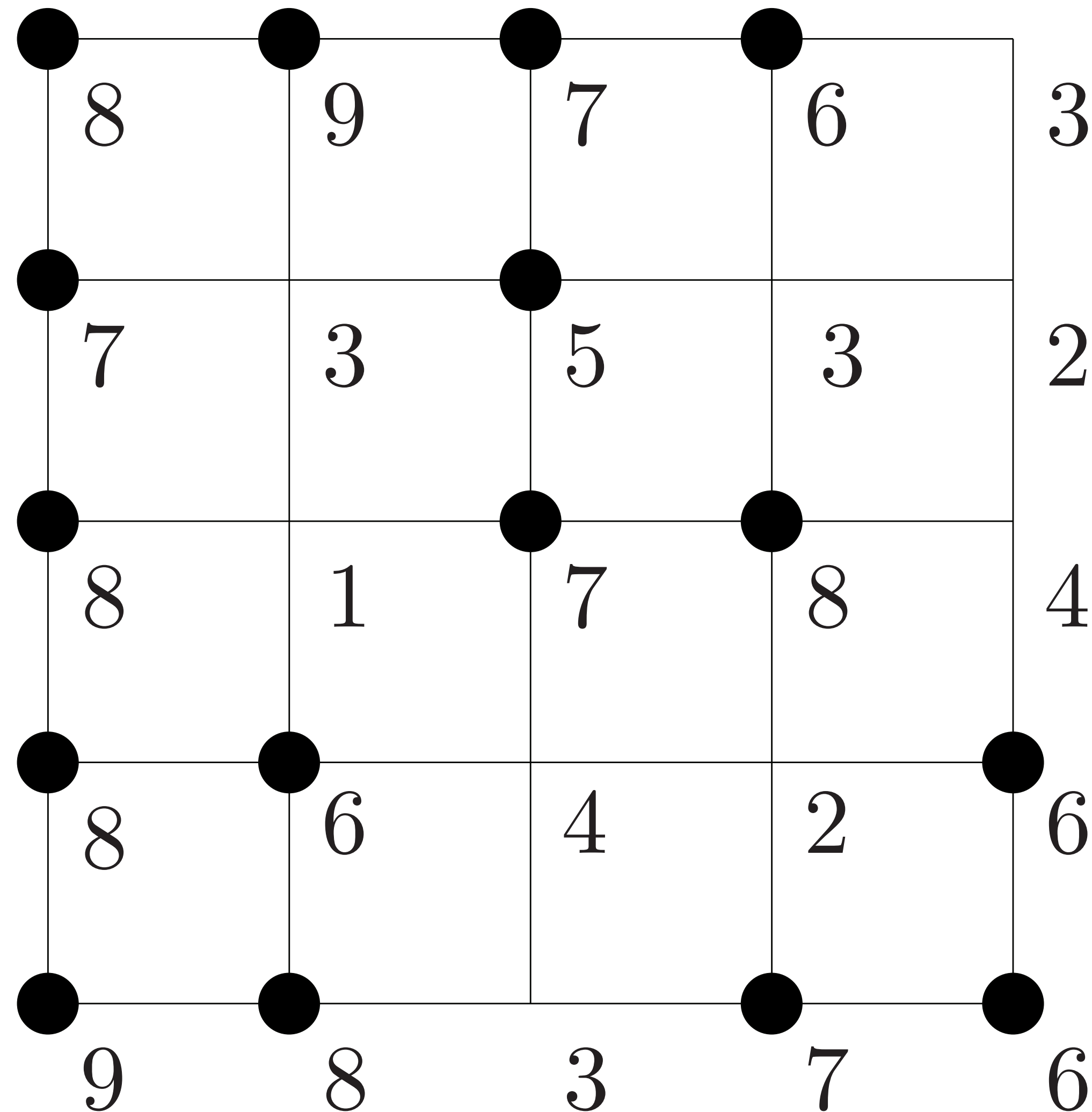
- Given an **isovalue**, we want to draw the isocontours corresponding to that value
- Remember we only have values defined at grid points
- How do we get isolines or isosurfaces from that data?
- Can we use the ideas from interpolation?

# Generating Isolines (Isovalue = 5)

8	9	7	6	3
7	3	5	3	2
8	1	7	8	4
8	6	4	2	6
9	8	3	7	6

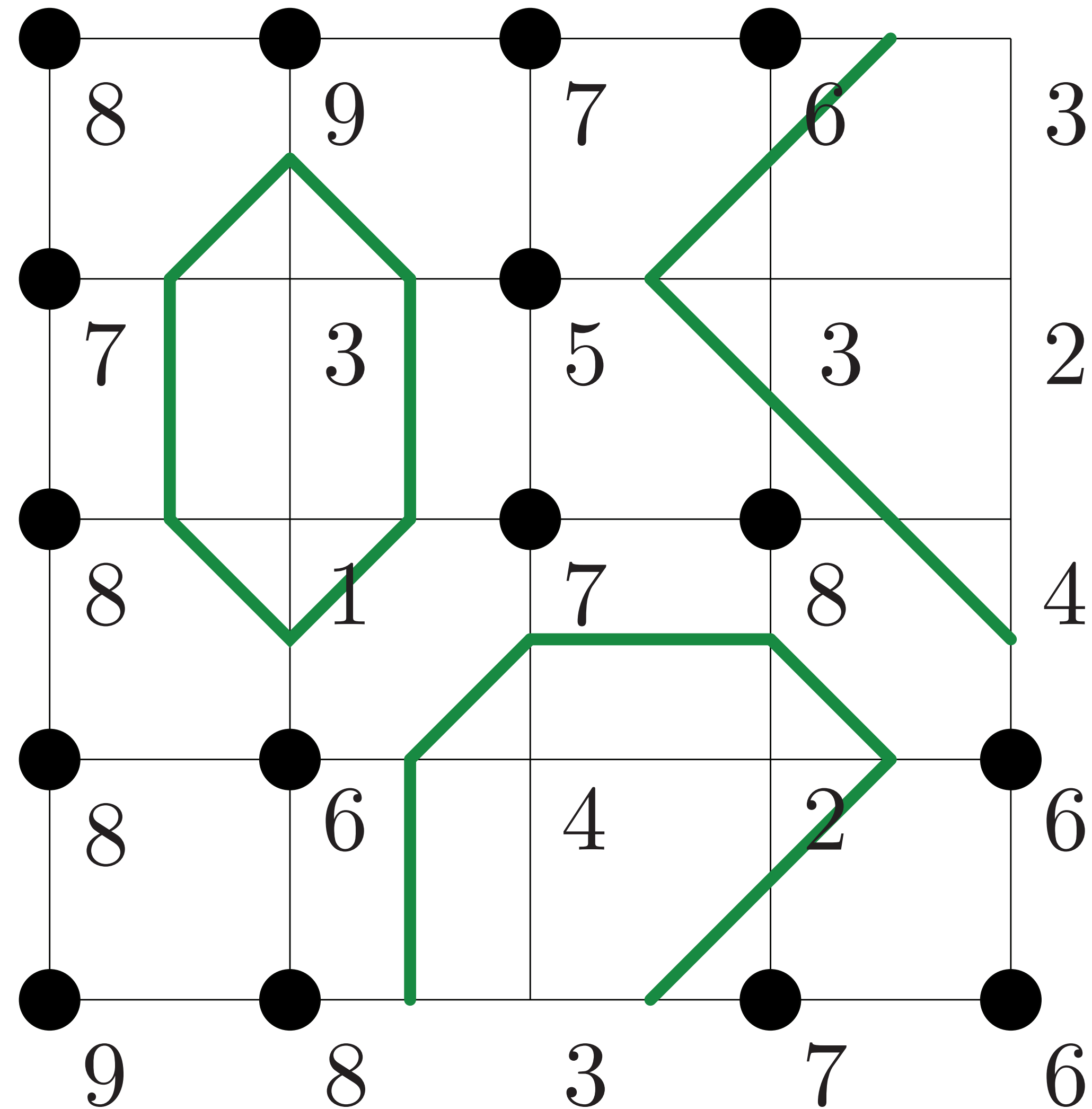
[R. Wenger, 2013]

# Generating Isolines



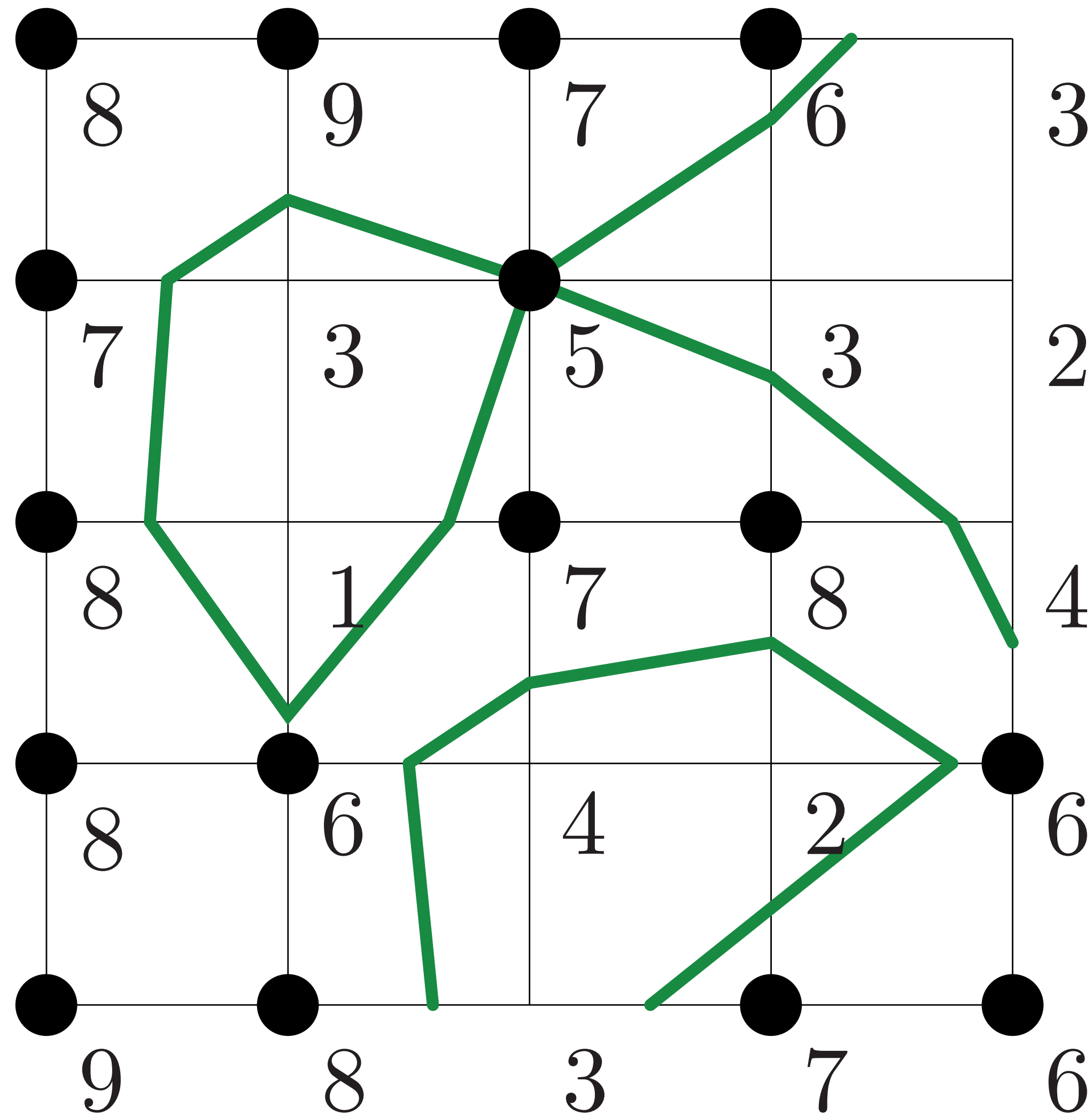
[R. Wenger, 2013]

# Generating Isolines



[R. Wenger, 2013]

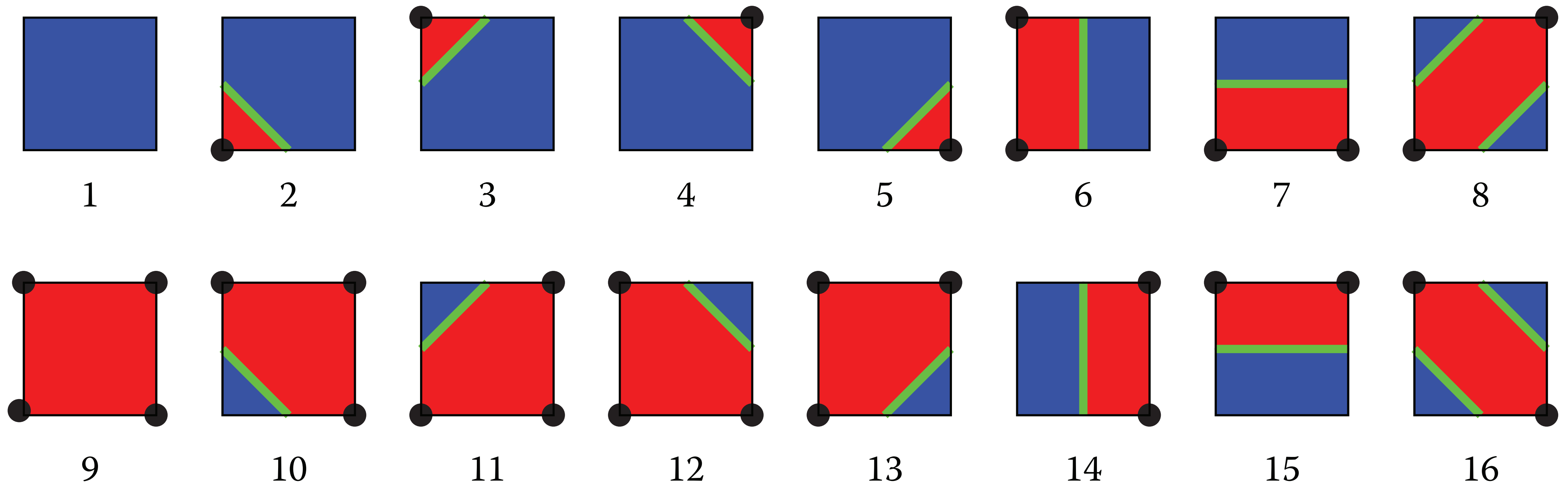
# Generating Isolines



[R. Wenger, 2013]



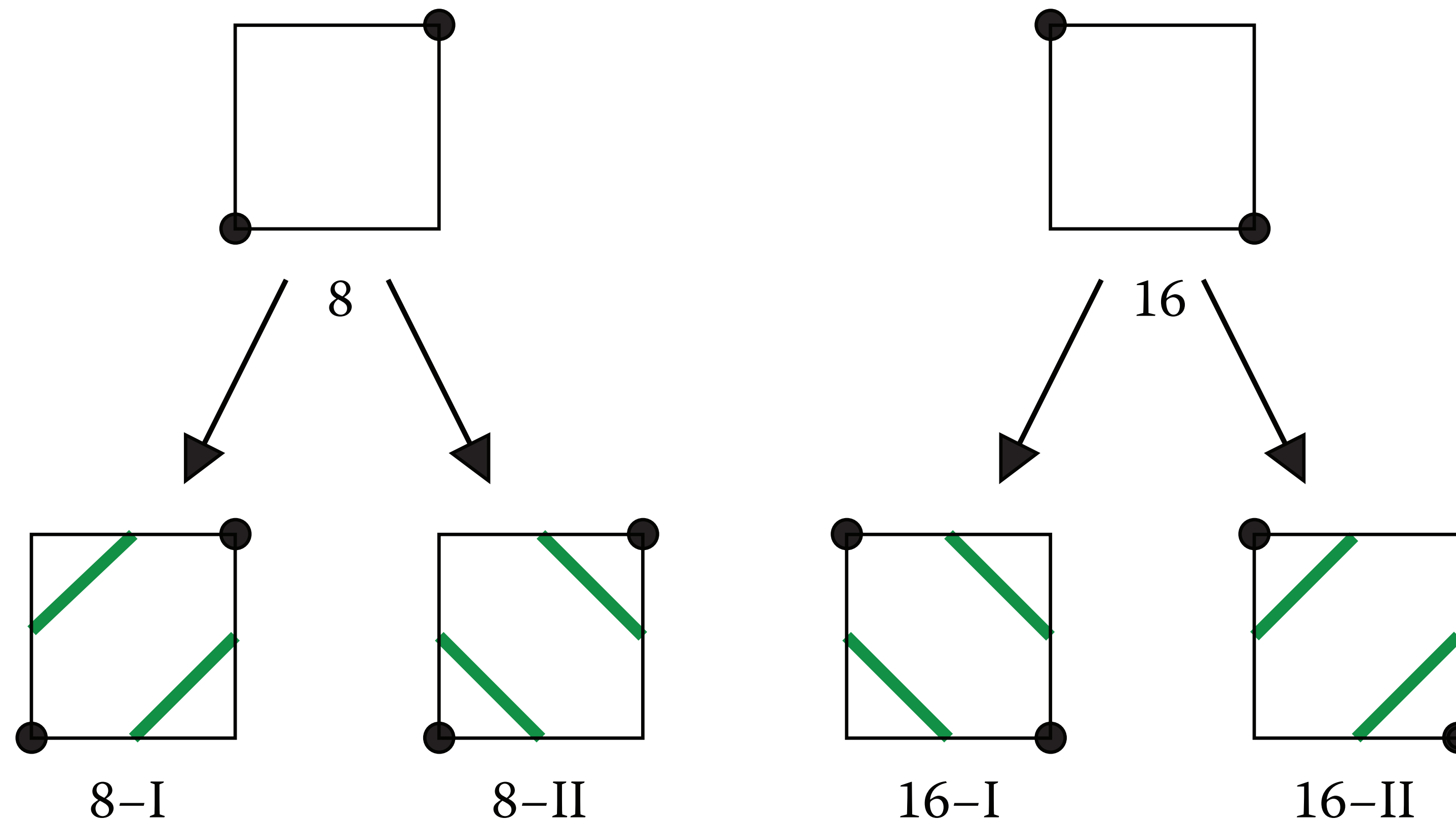
# Marching Squares



[R. Wenger, 2013]

# Ambiguous Configurations

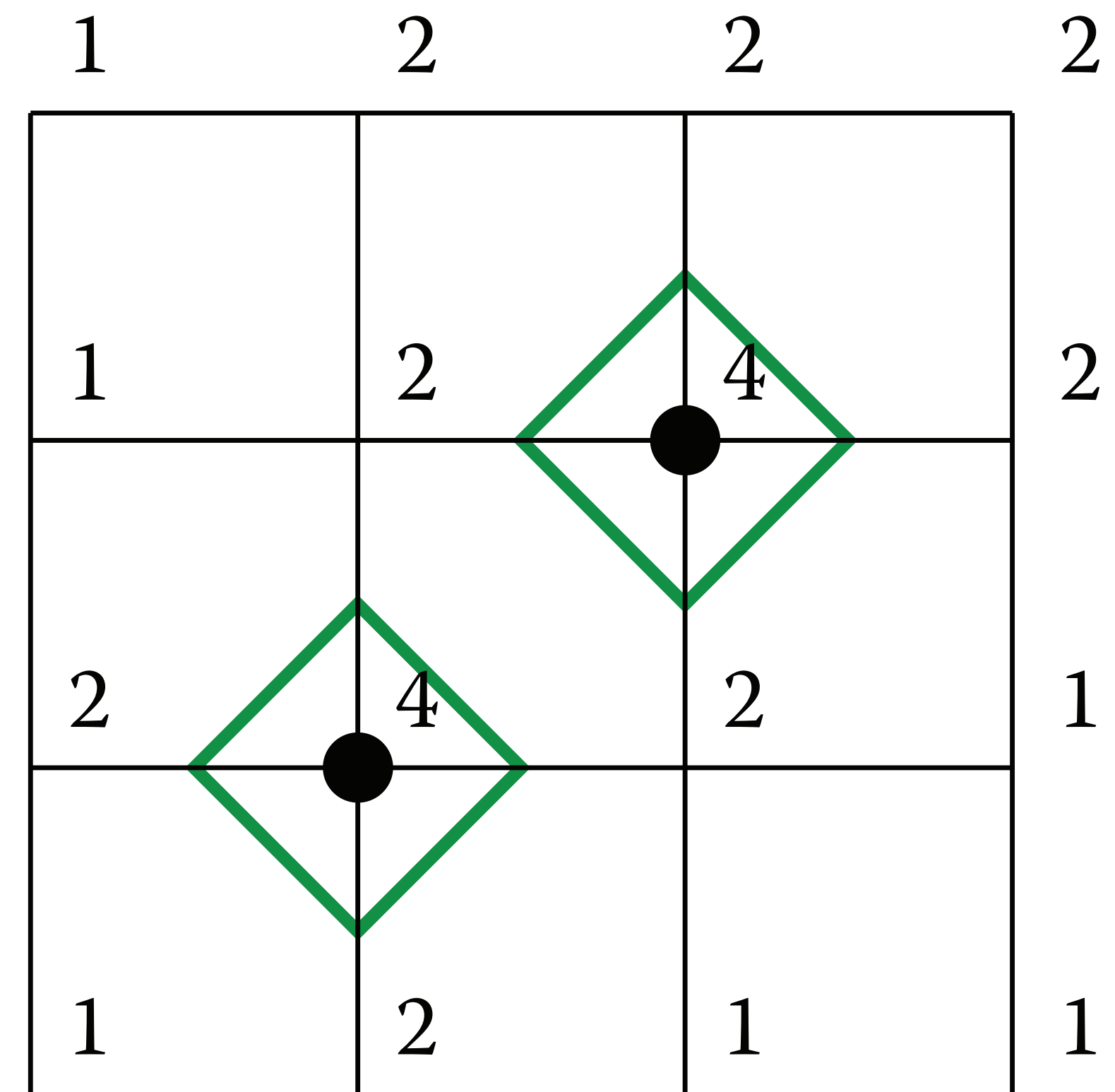
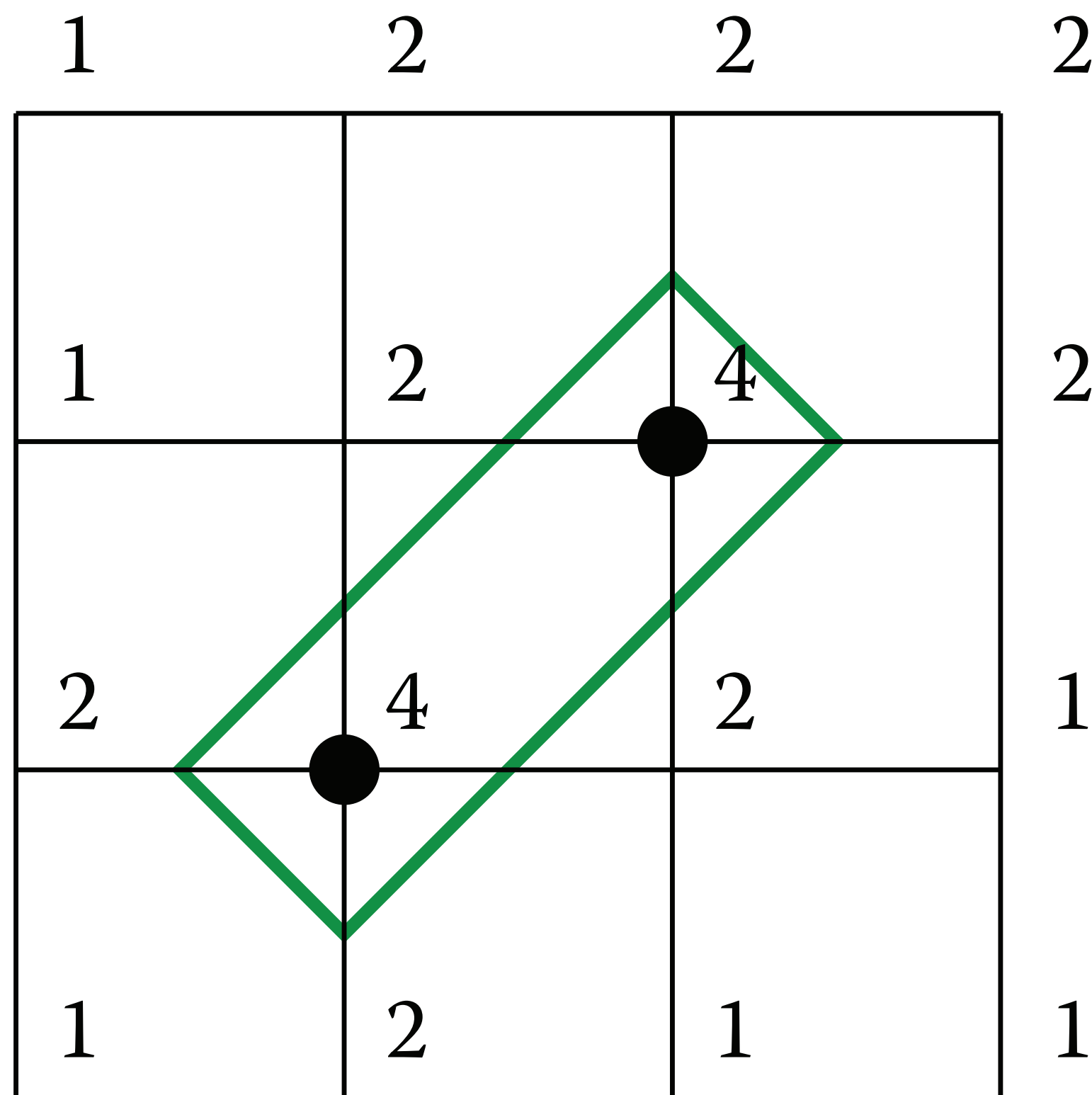
- There are some cases for which we cannot tell which way to draw the isolines...



[R. Wenger, 2013]

# Ambiguous Configurations

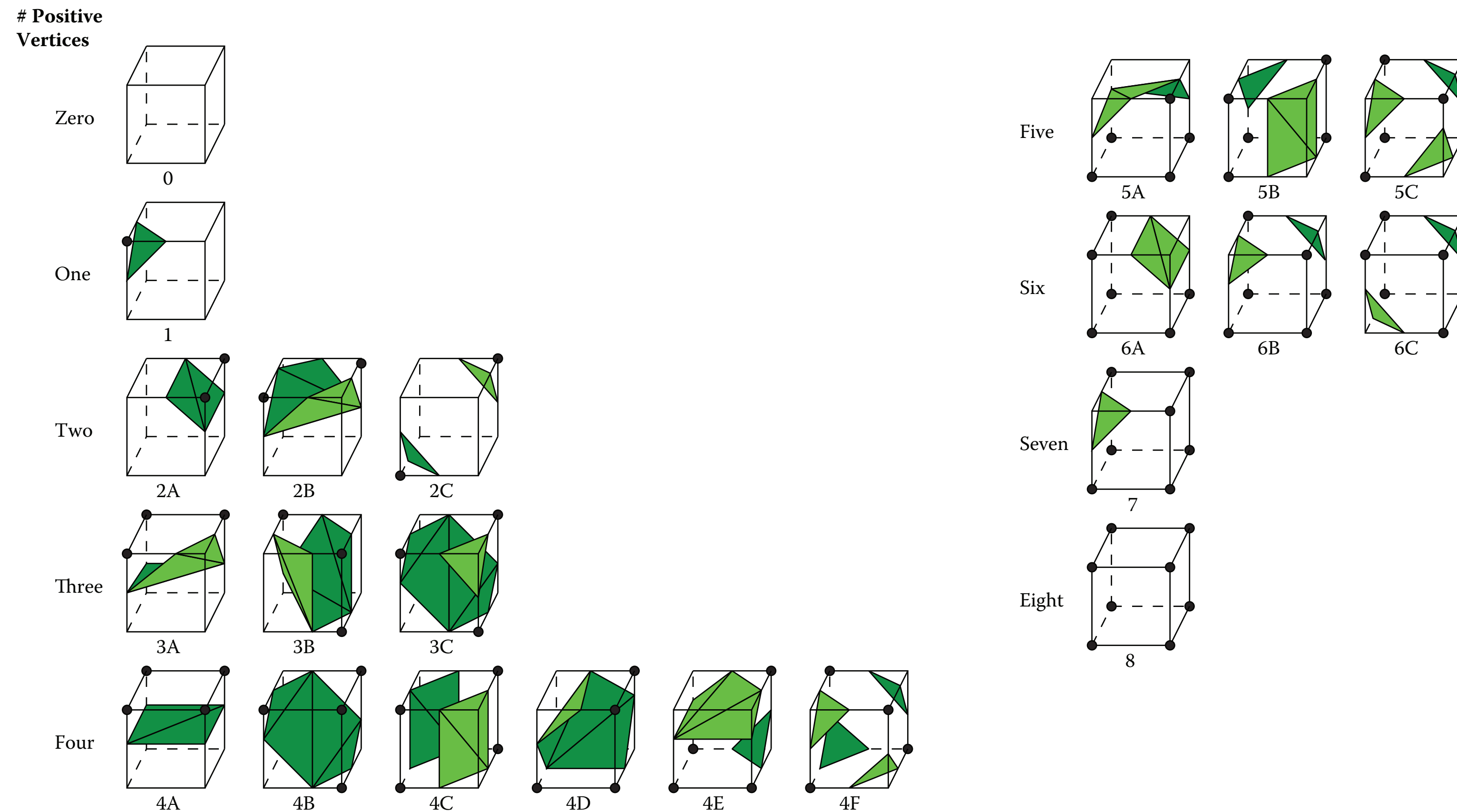
- Either works for marching squares, this isn't the case for 3D



[R. Wenger, 2013]

# 3D: Marching Cubes

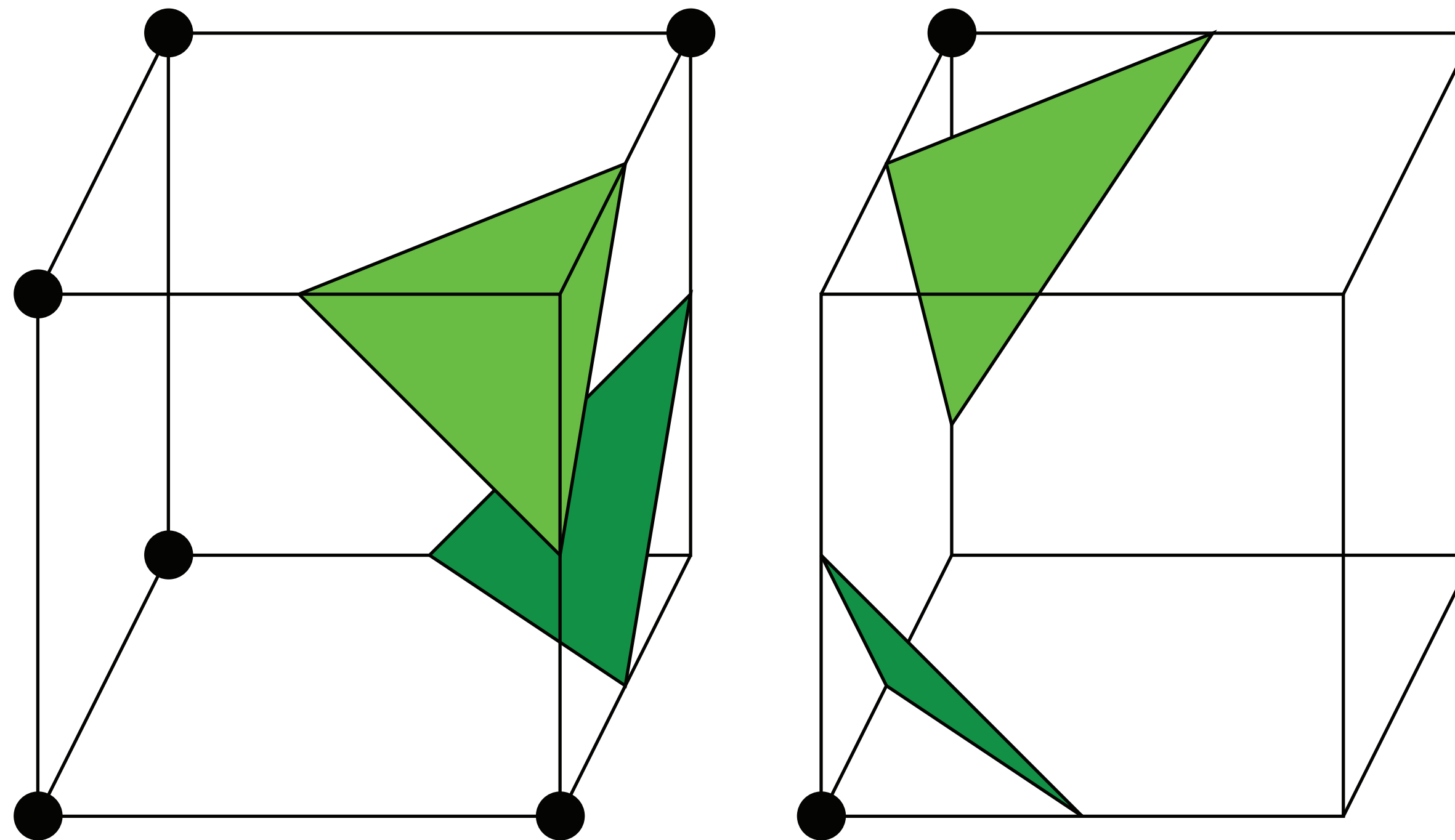
- Same idea, more cases [Lorensen and Cline, 1987]



[R. Wenger, 2013]

# Incompatible Choices

- If we have ambiguous cases where we choose differently for each cell, the surfaces will not match up correctly—there are holes
- Fix with the **asymptotic decider** [Nielson and Hamann, 1991]



[R. Wenger, 2013]

# Marching Cubes Algorithm

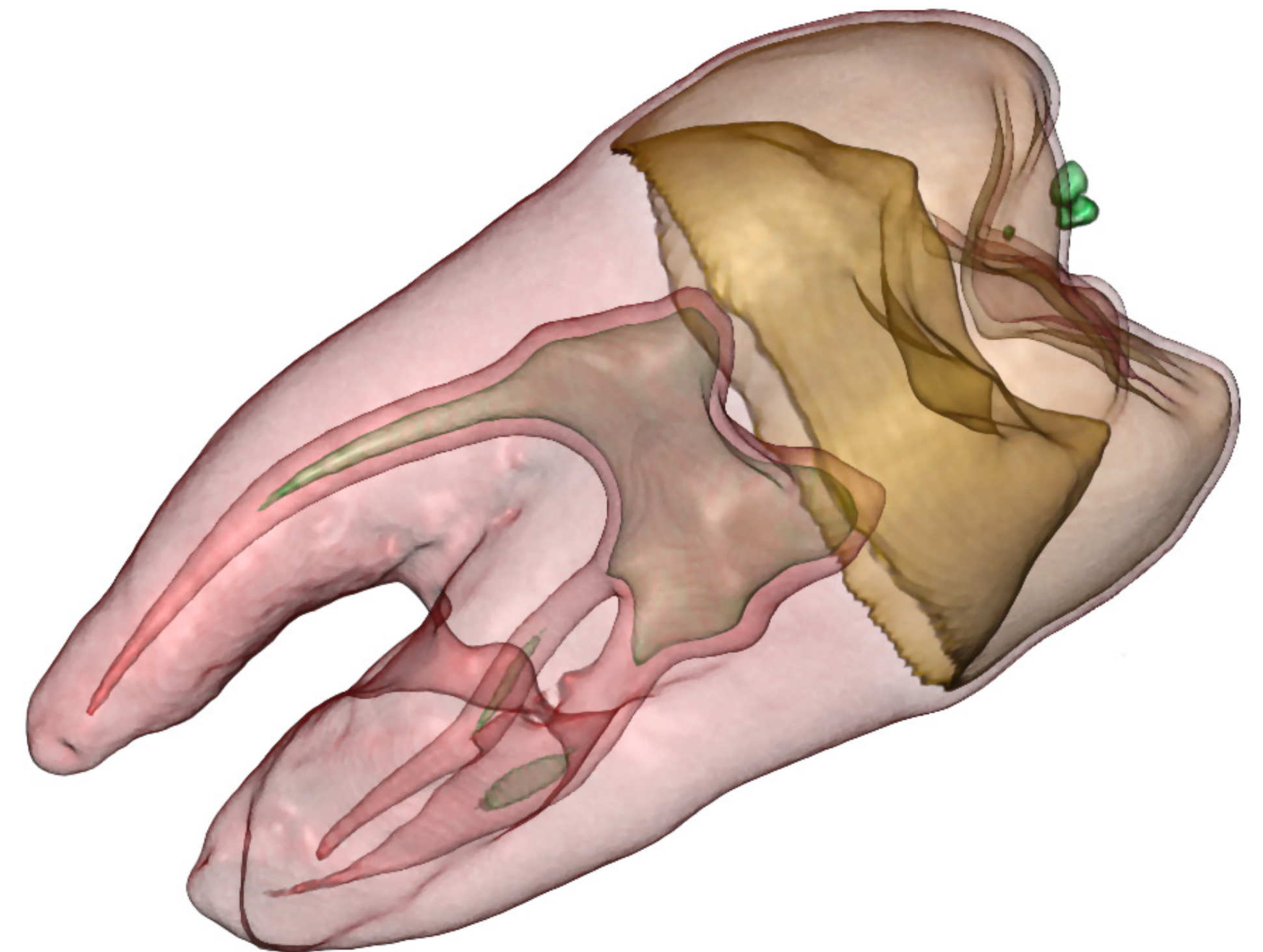
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- For each cell:
  - Classify each vertex as inside or outside ( $\geq$ ,  $<$ ) — 0 or 1
  - Take the eight vertex classifications as a bit string
  - Use the bit string as a lookup into a table to get edges
  - Interpolate to get actual edge locations
  - Compute gradients
  - Resolve ambiguities
- Render a bunch of triangles: easy for graphics cards



# Multiple Isosurfaces

- Topographical maps have multiple isolines to show elevation trends
- Problem in 3D? **Occlusion**
- Solution? Transparent surfaces
- Issues:
  - Think about color in order to make each surface visible
  - Compositing: how do colors "add up" with multiple surfaces
  - How to determine good isovalues?



[J. Kniss, 2002]



# Volume Rendering

# Volume Rendering vs. Isosurfacing

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(a) Direct volume rendered



(b) Isosurface rendered

[Kindlmann, 1998]

# (Direct) Volume Rendering

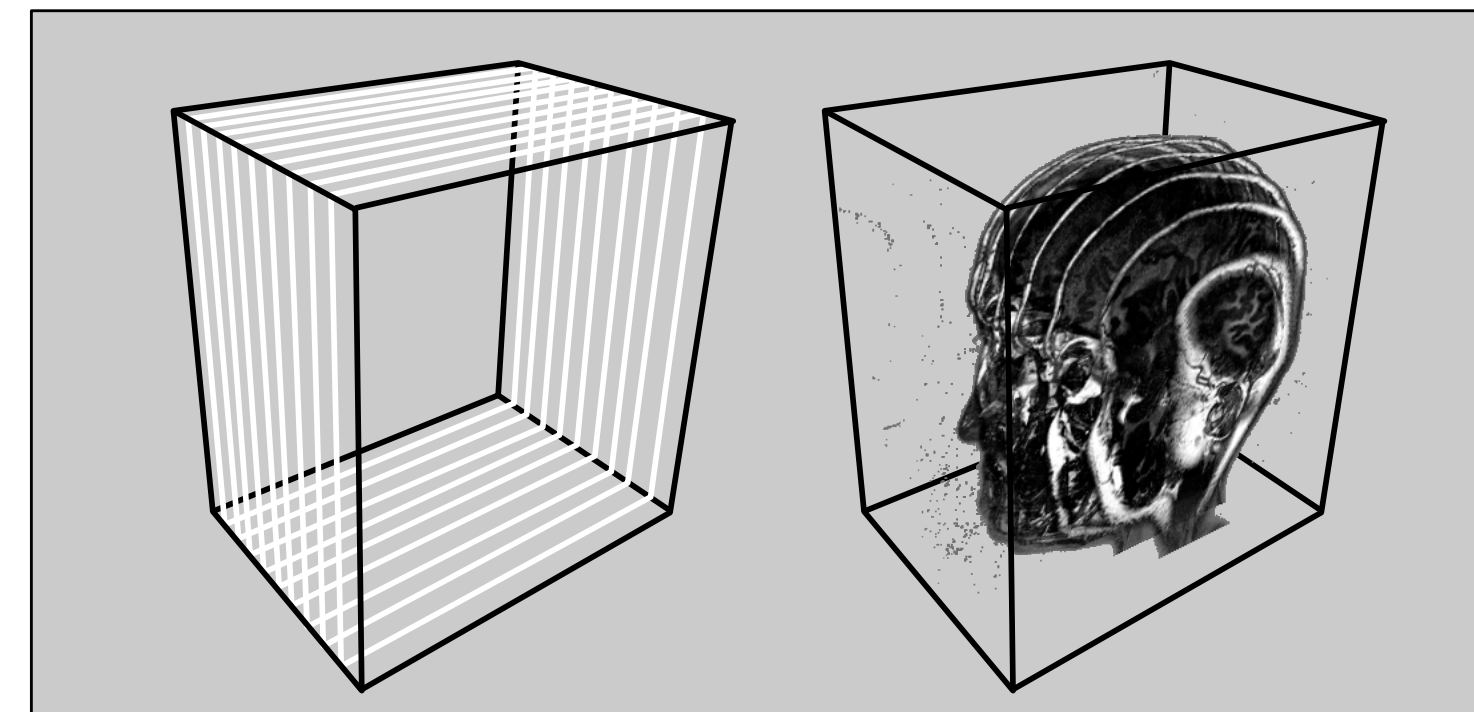
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- Isosurfacing: compute a surface (triangles) and use standard computer graphics to render the triangles
- Volume rendering: compute the pixels shown directly from the volume information
- Why?
  - No need to figure out precise isosurface boundaries
  - Can work better for data with noise or uncertainty
  - Greater control over appearance based on values

# Types of Volume Rendering Algorithms

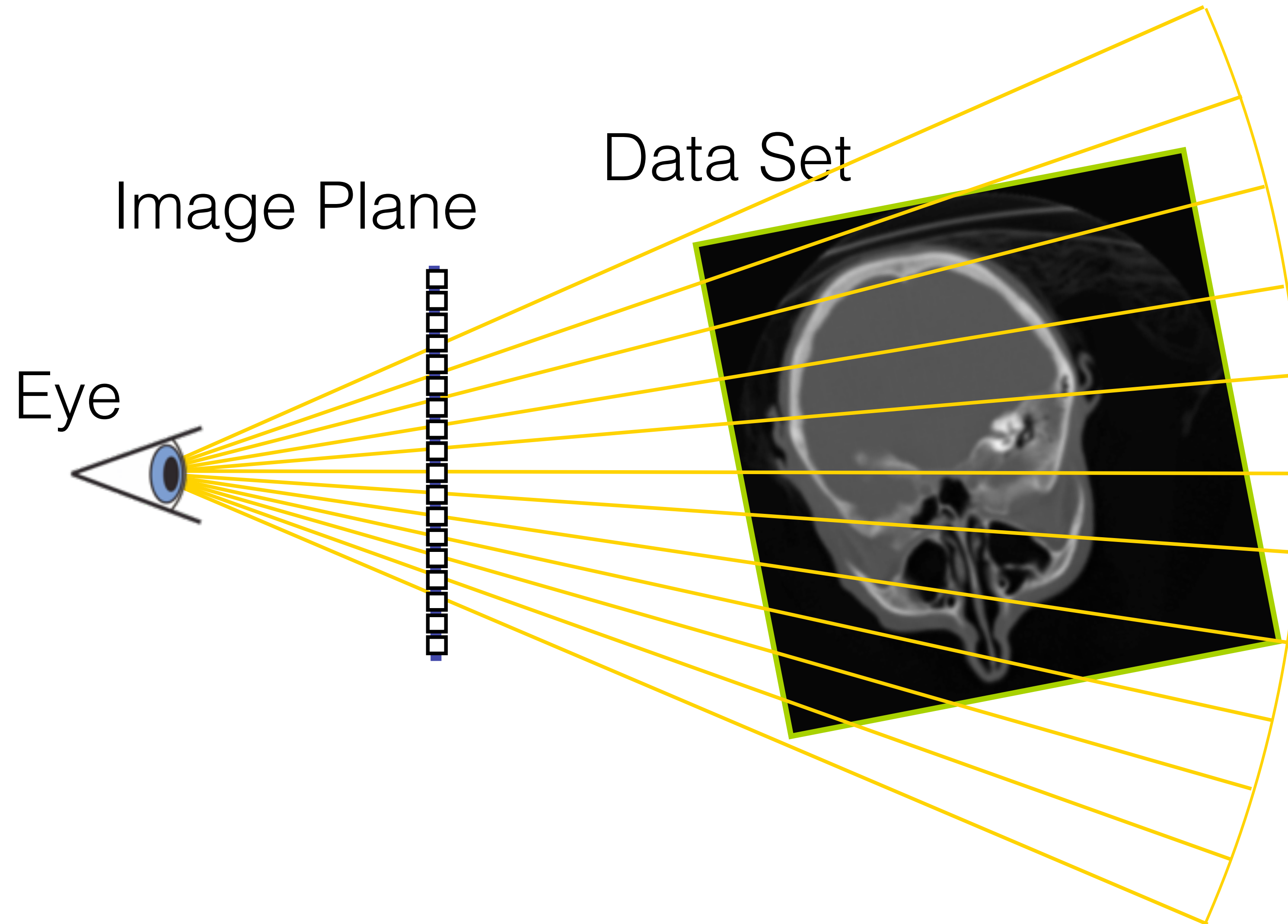
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- Ray casting
  - Similar to ray tracing, but use rays from the viewer
- Splatting:
  - Object-order, voxels splat onto the image plane
- Shear Warp:
  - Object-space, slice-based, parallel viewing rays
- Texture-Based:
  - 2D Slices: stack of texture maps
  - 3D Textures



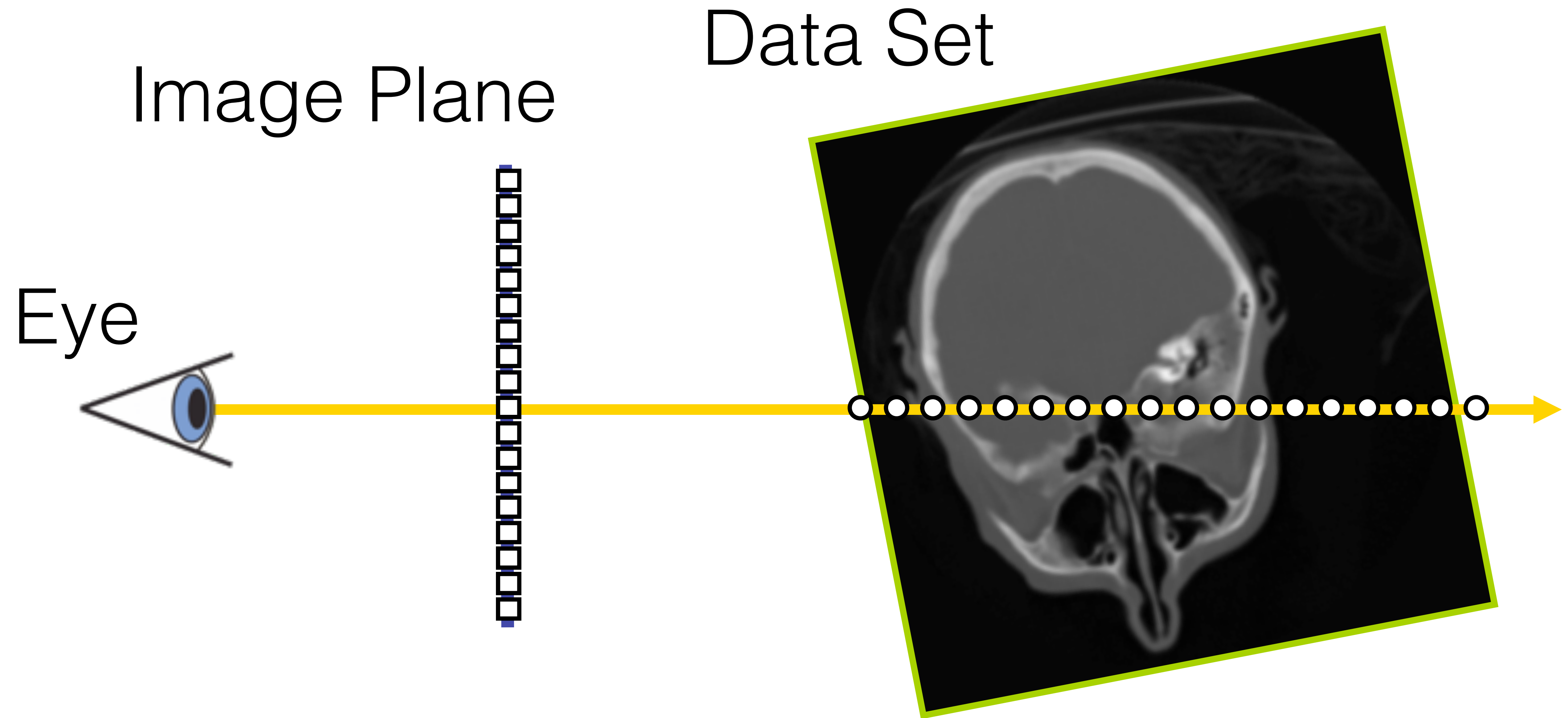
[via Möller]

# Volume Ray Casting



[Levine]

# Volume Ray Casting

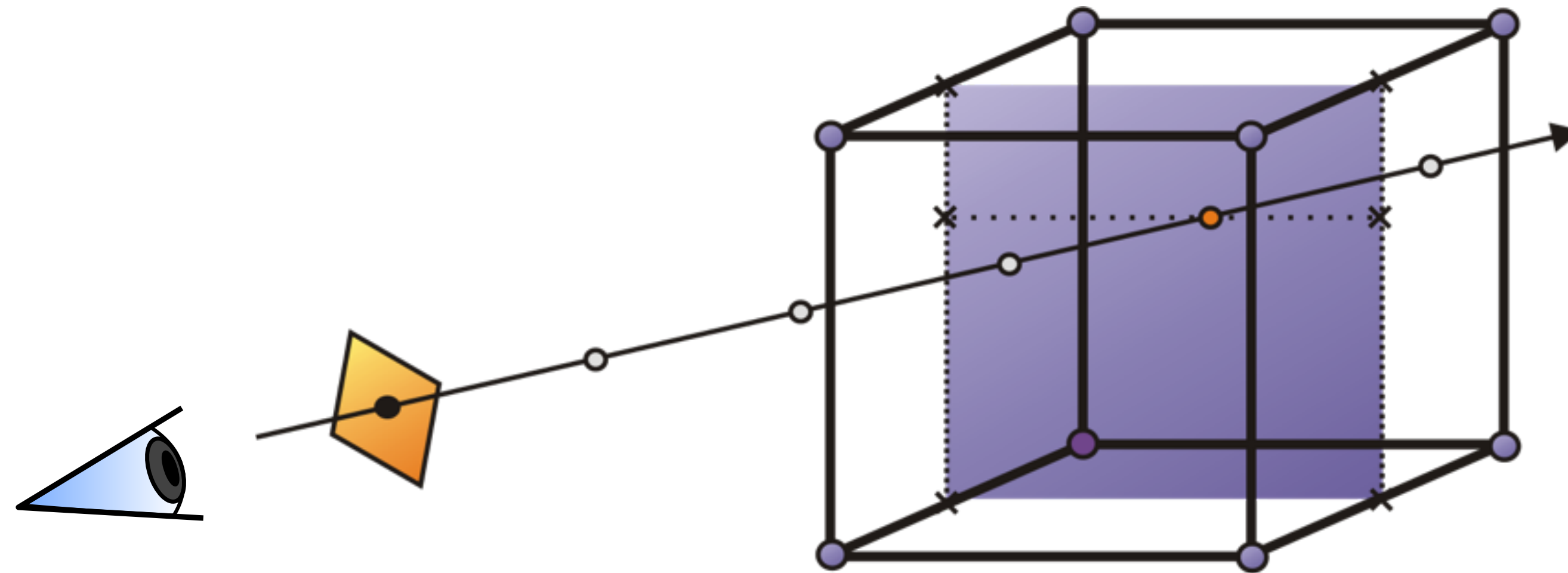


[Levine]



# How?

- Approximate volume rendering integral: light absorption & emission
- Sample at regular intervals along each ray
- Trilinear interpolation: linear interpolation along each axes (x,y,z)

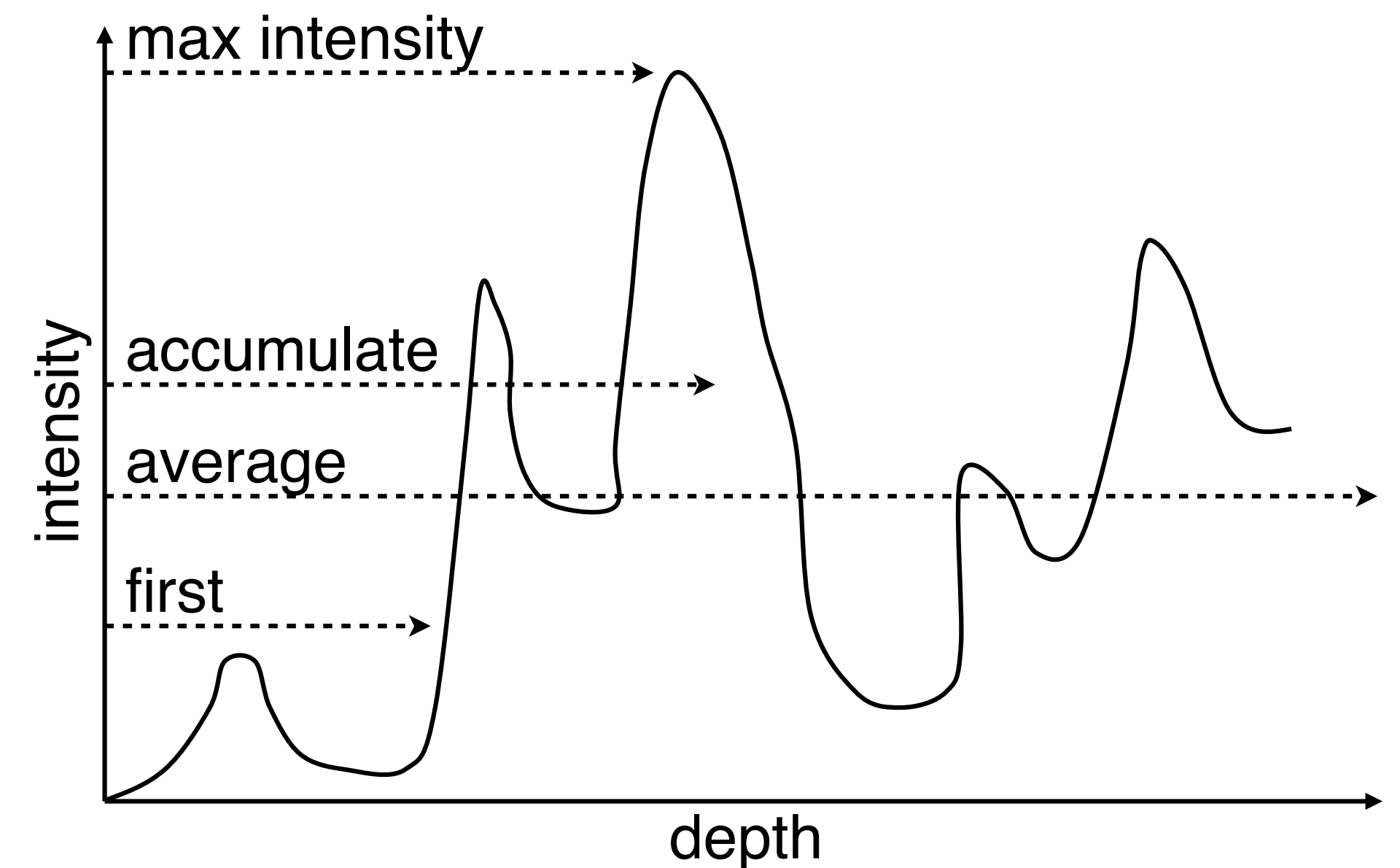


- Not the only possibility, also "object order" techniques like splatting or texture-based and combinations like shear-warp



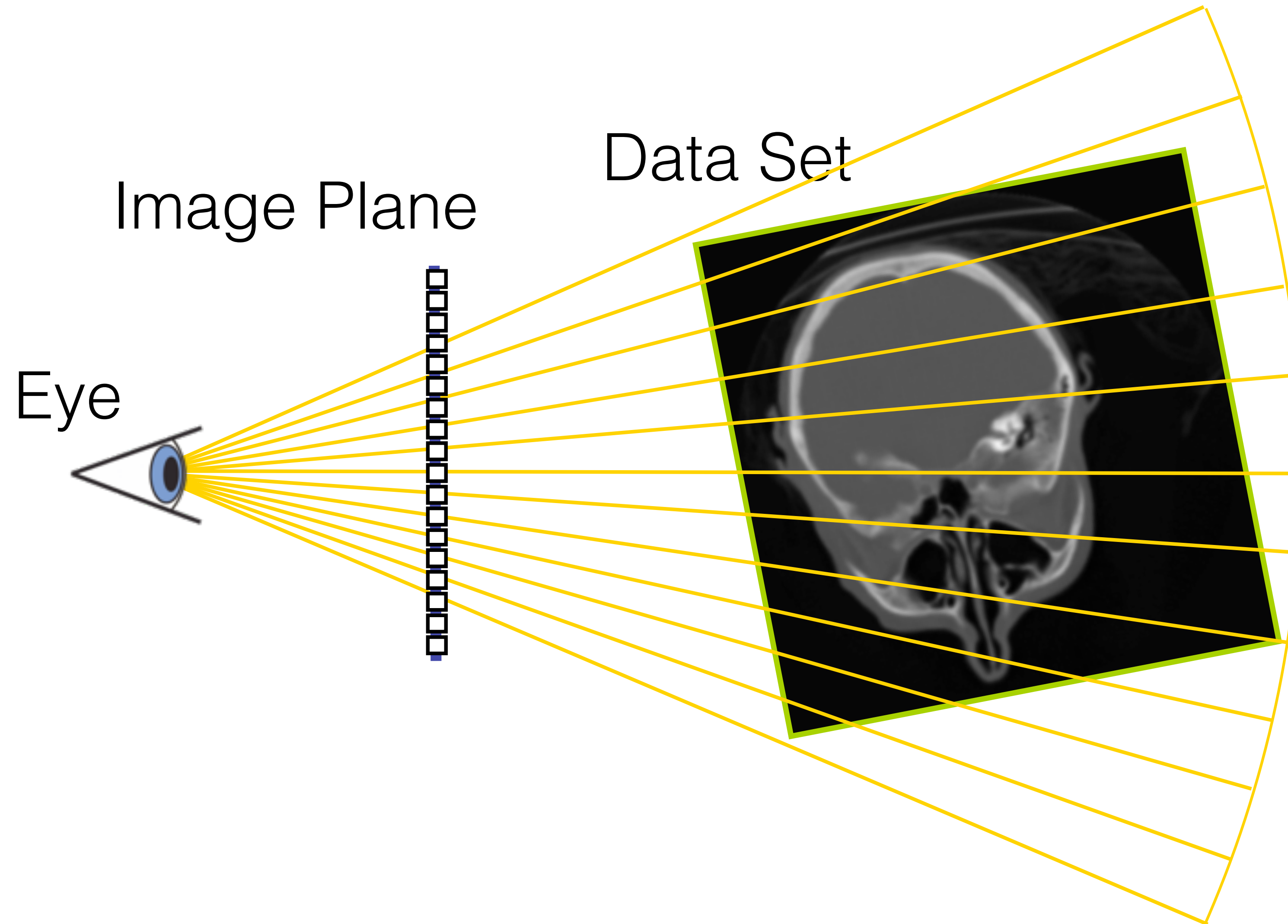
# Compositing

- Need **one pixel** from all values along the ray
- Q: How do we "add up" all of those values along the ray?
- A: Compositing!
- Different types of compositing
  - First: like isosurfacing, first intersection at a certain intensity
  - Max intensity: choose highest val
  - Average: mean intensity (density, like x-rays)
  - Accumulate: each voxel has some contribution



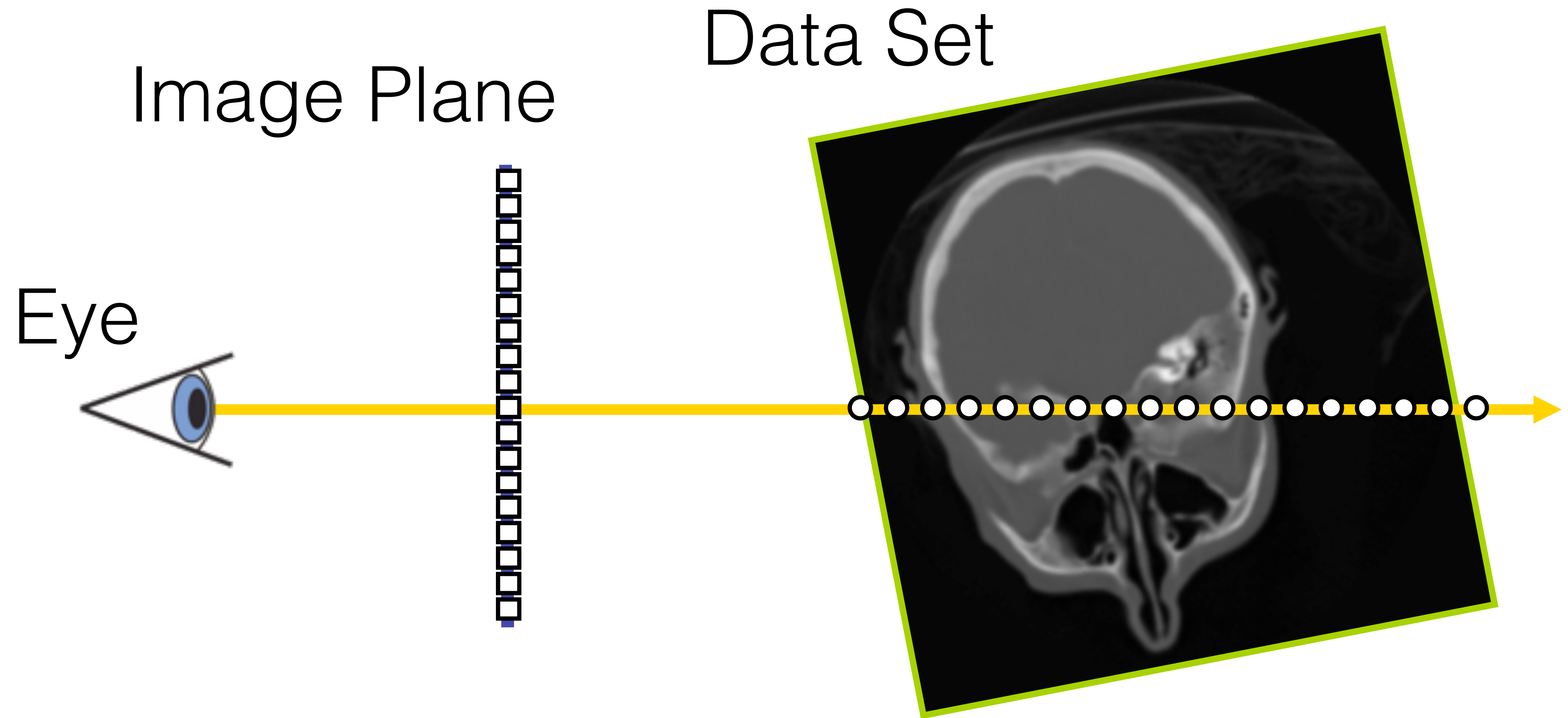
[Levine and Weiskopf/Machiraju/Möller]

# Volume Ray Casting



[Levine]

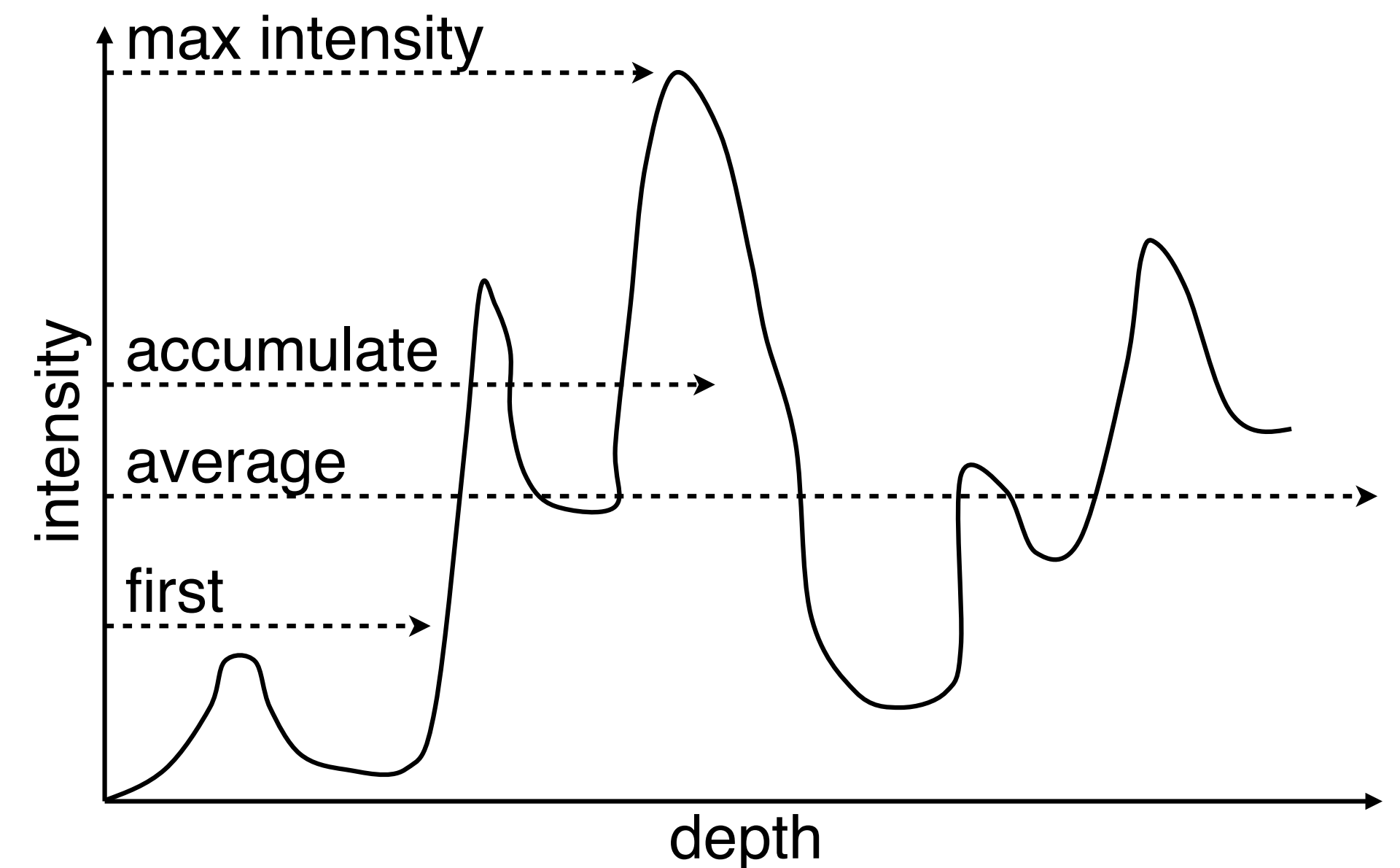
# Volume Ray Casting



[Levine]

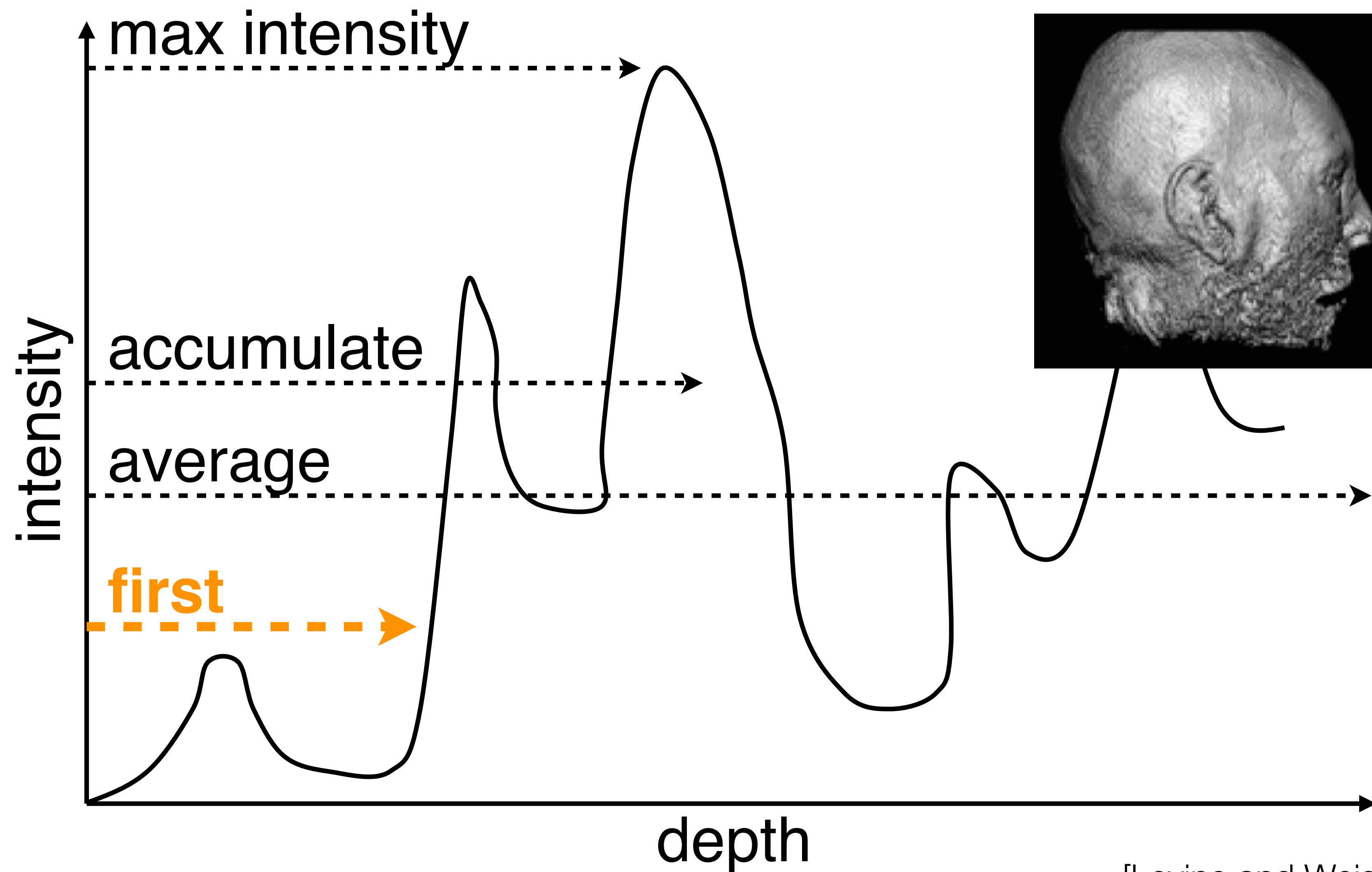
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[Levine and Weiskopf/Machiraju/Möller]

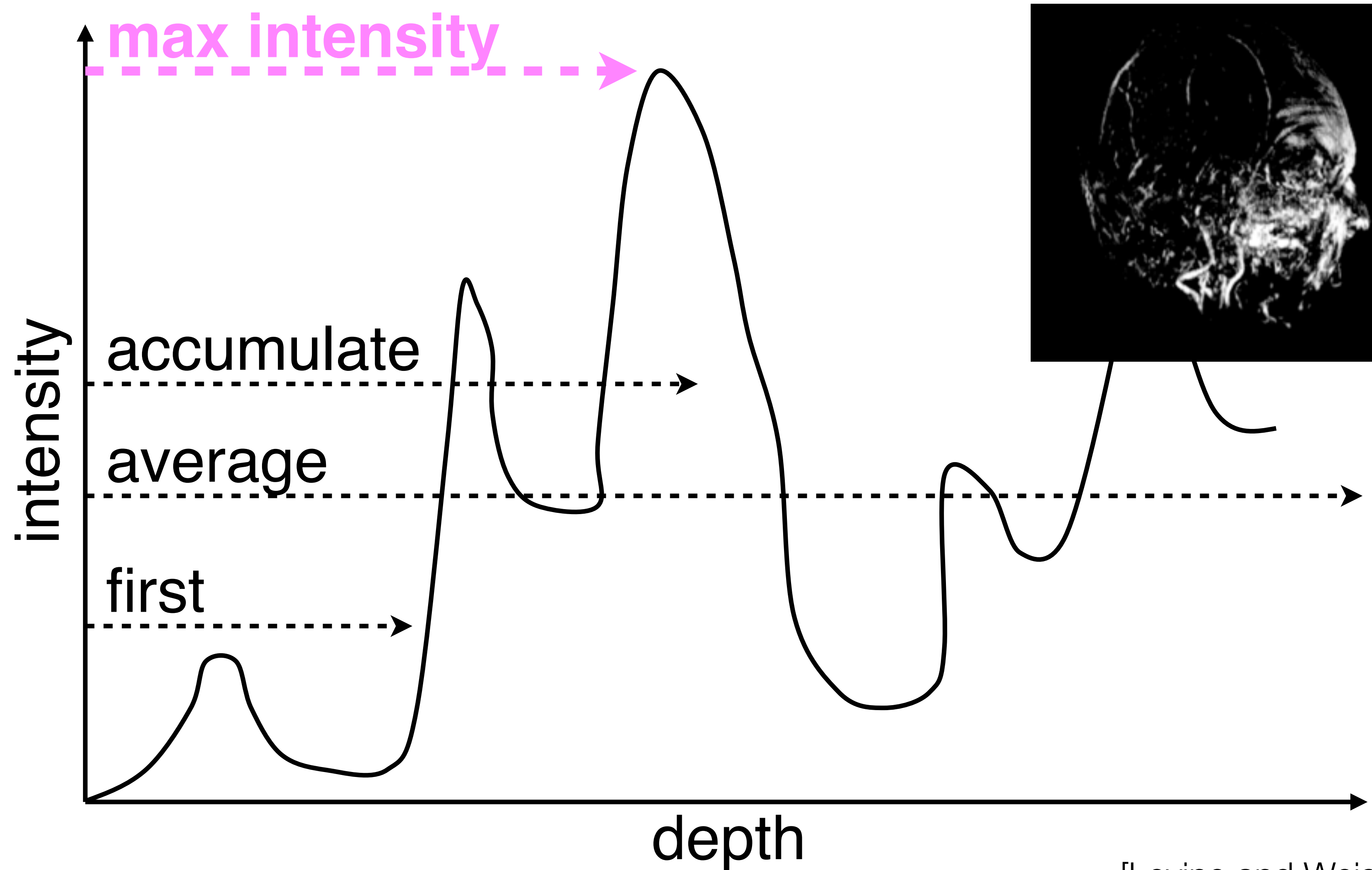
# Types of Compositing



[Levine and Weiskopf/Machiraju/Möller]

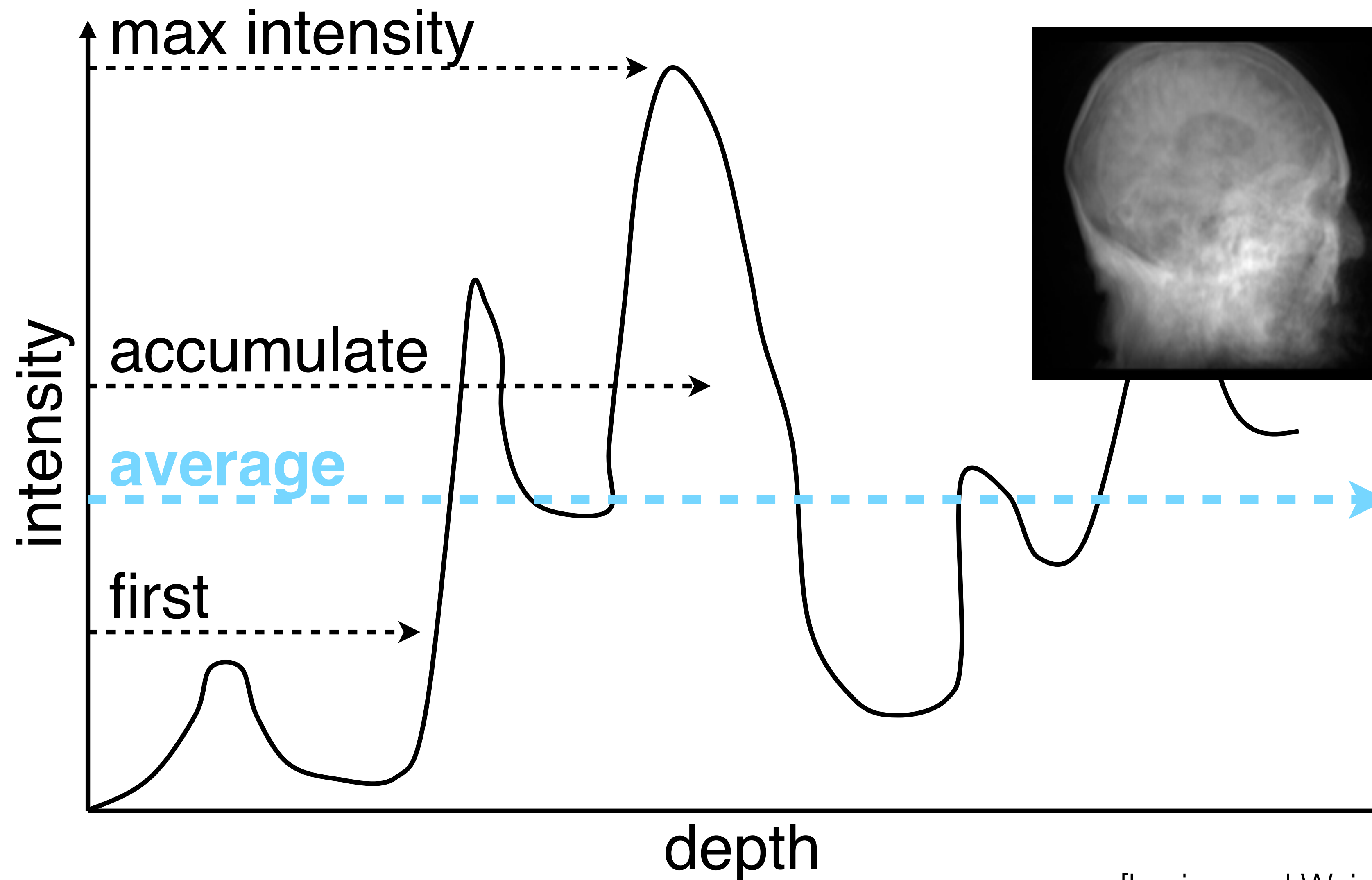


# Types of Compositing



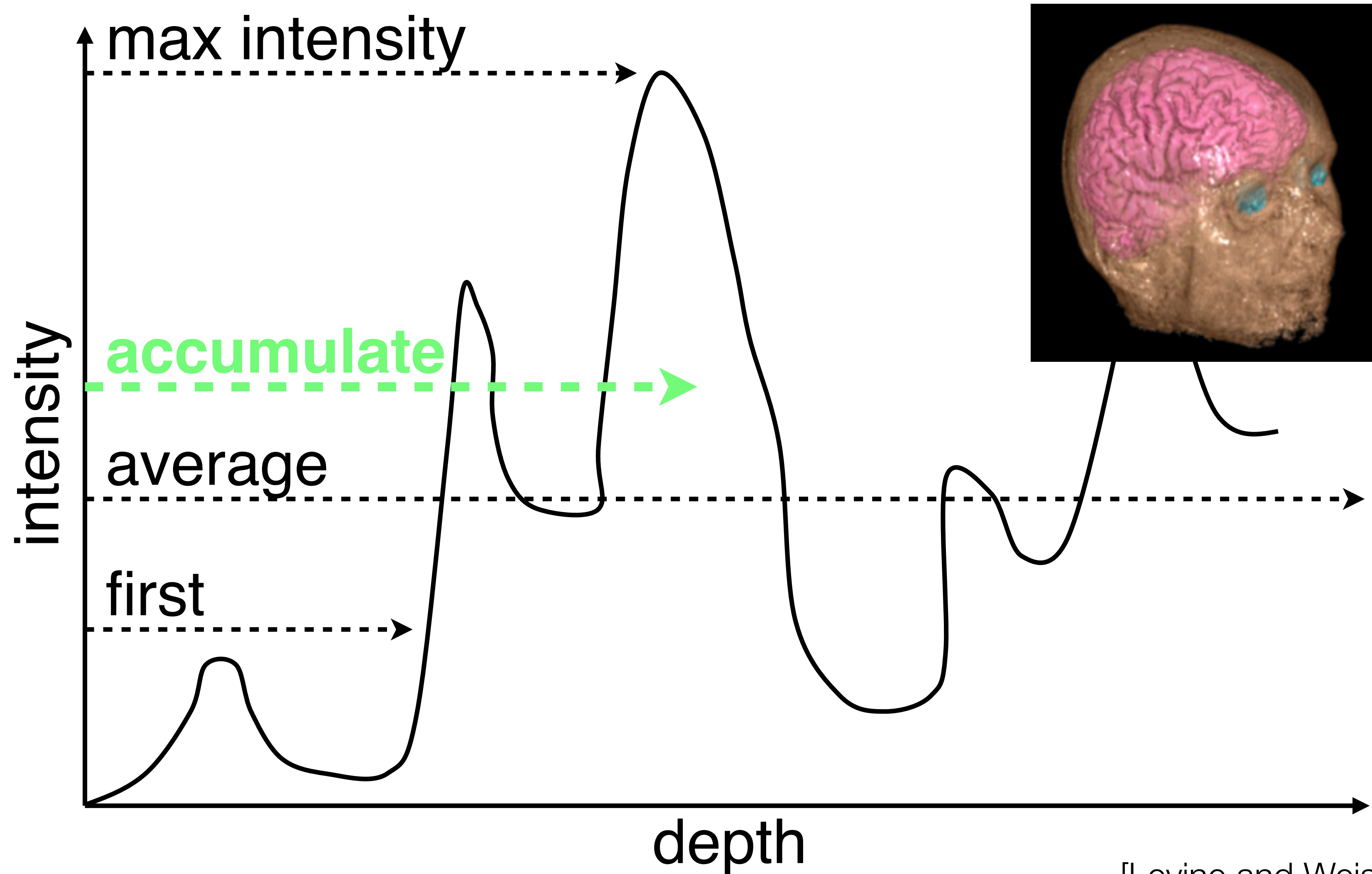
[Levine and Weiskopf/Machiraju/Möller]

# Types of Compositing



[Levine and Weiskopf/Machiraju/Möller]

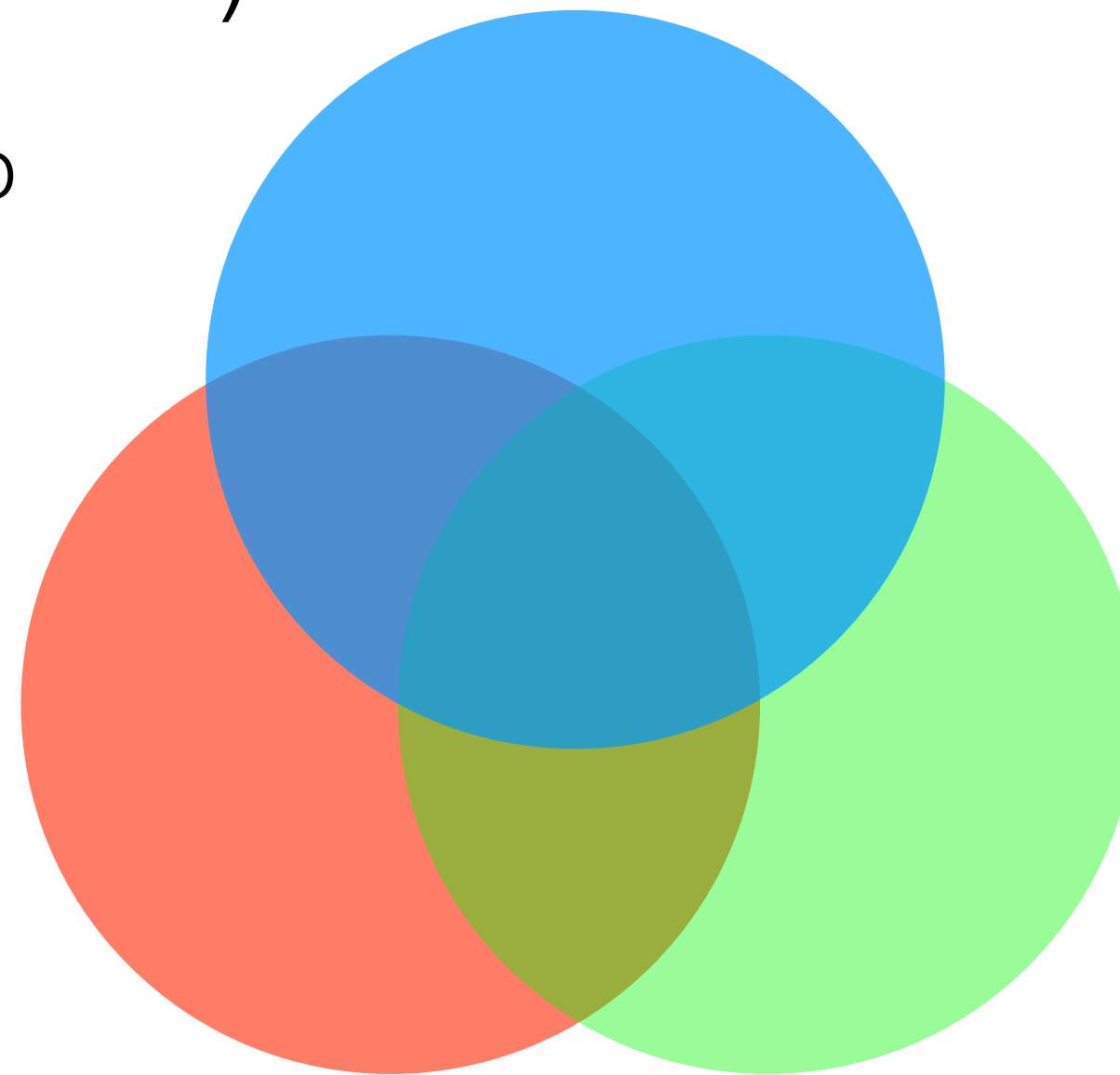
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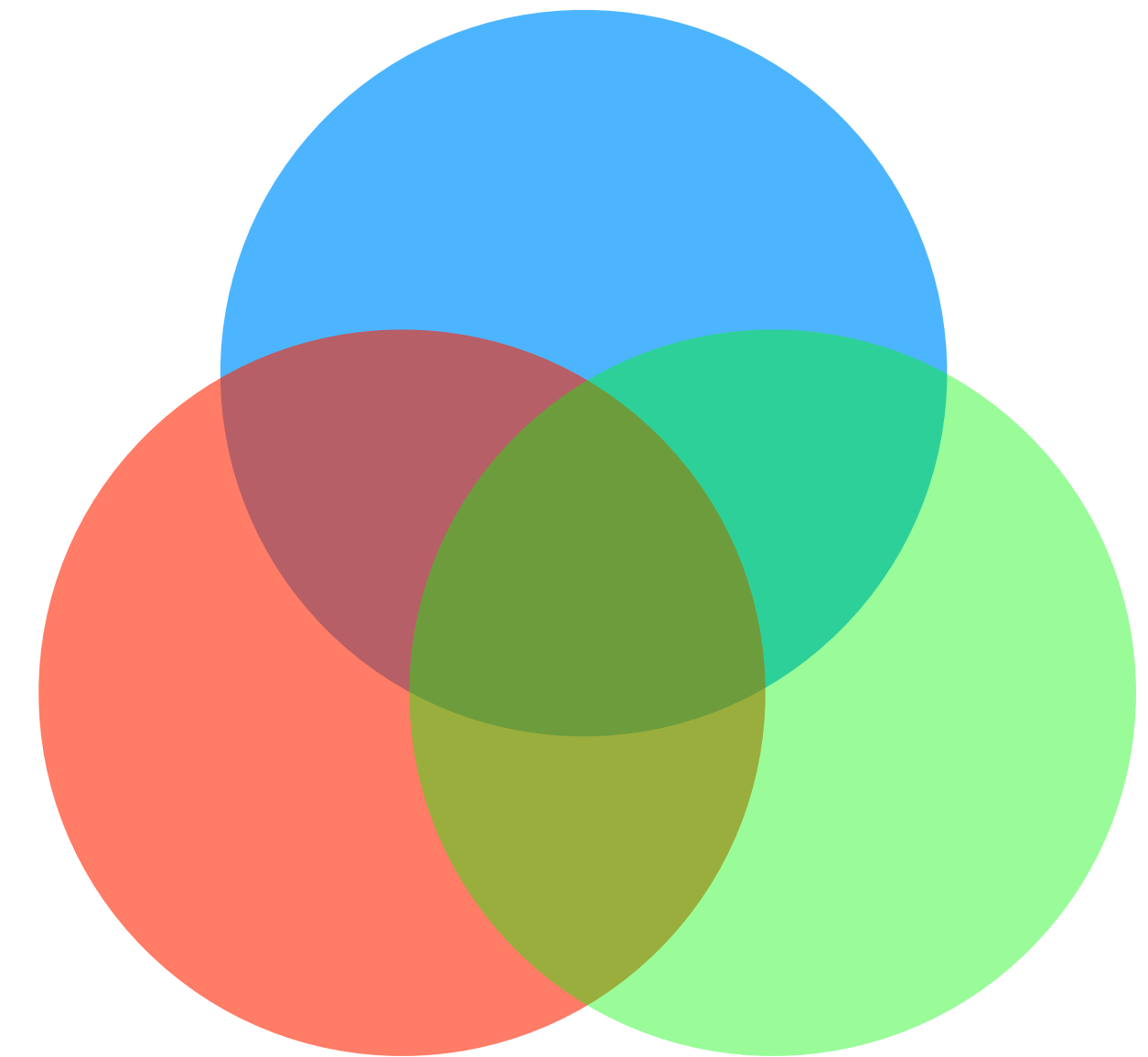
[Levine and Weiskopf/Machiraju/Möller]

# Accumulation

- If we're not just calculating a single number (max, average) or a position (first), how do we determine the accumulation?
- Assume each value has an associated color ( $c$ ) and opacity ( $\alpha$ )
- Over operator (back-to-front):
  - $c = \alpha_f \cdot c_f + (1 - \alpha_f) \cdot \alpha_b \cdot c_b$
  - $\alpha = \alpha_f + (1 - \alpha_f) \cdot \alpha_b$
- Order is important!



Blue Last

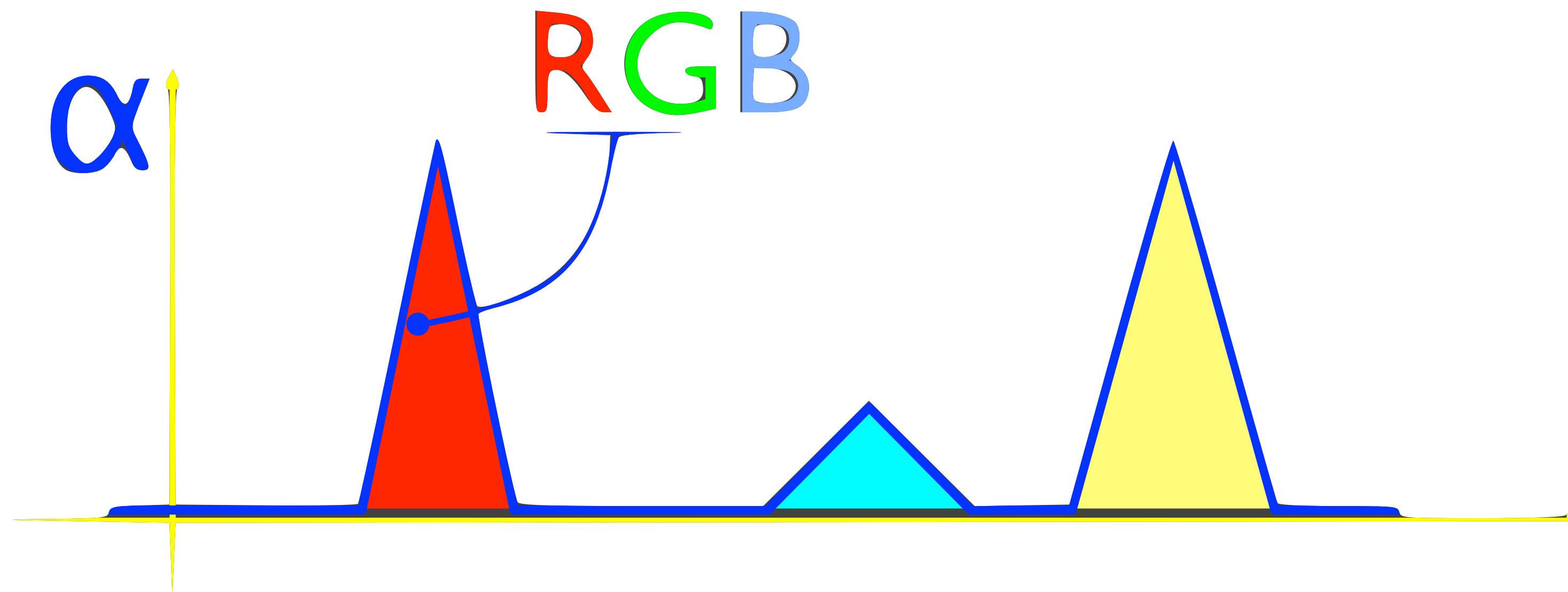


Blue First



# Transfer Functions

- Where do the colors and opacities come from?
- Idea is that each voxel emits/absorbs light based on its scalar value
- ...but users get to choose how that happens
- x-axis: color region definitions, y-axis: opacity



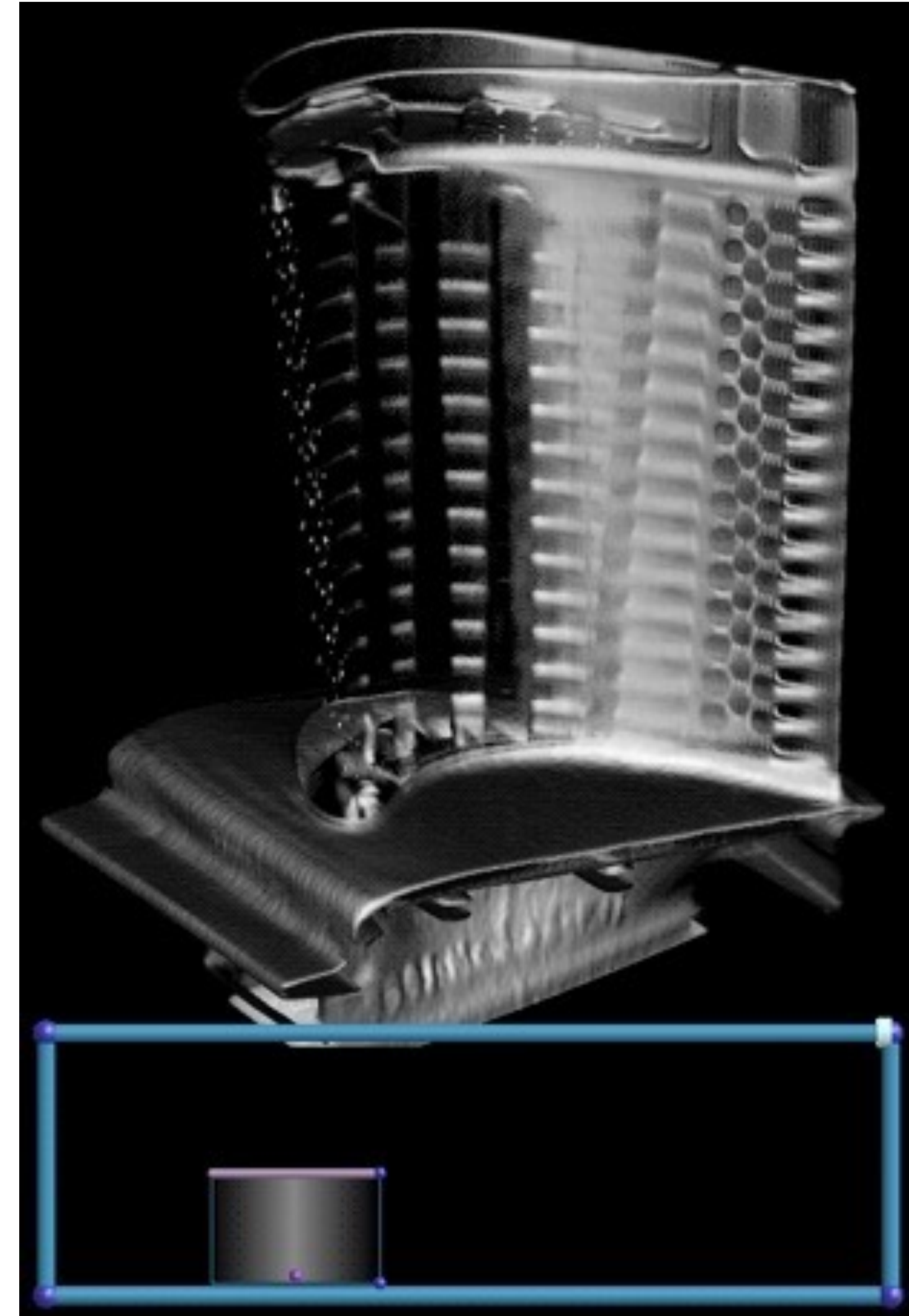
[Kindlmann]

# Transfer Function Design

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- Transfer function **design** is non-trivial!
- Lots of tools to help visualization designers to create good transfer functions
- Histograms, more attributes than just value like gradient magnitude

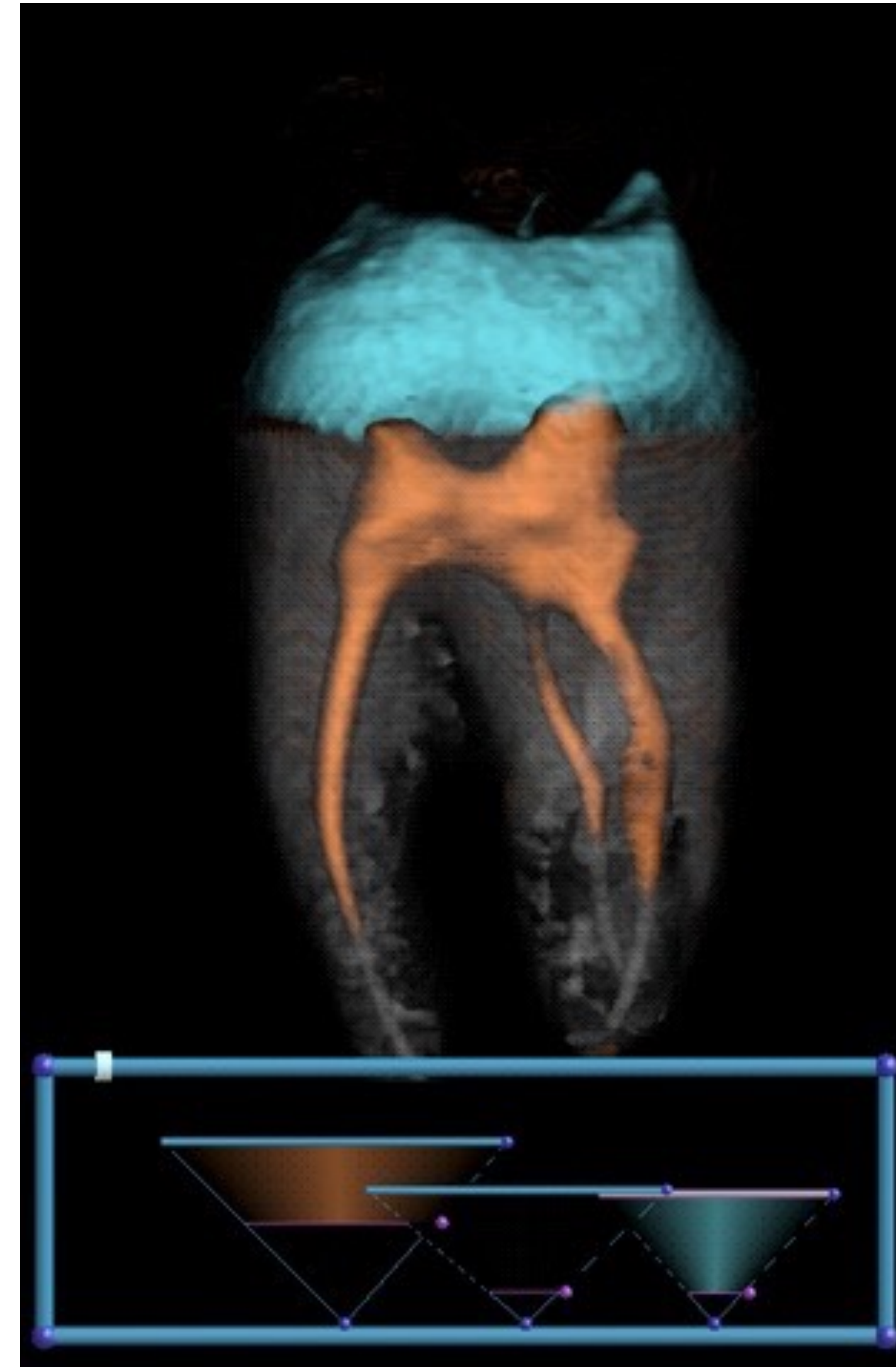
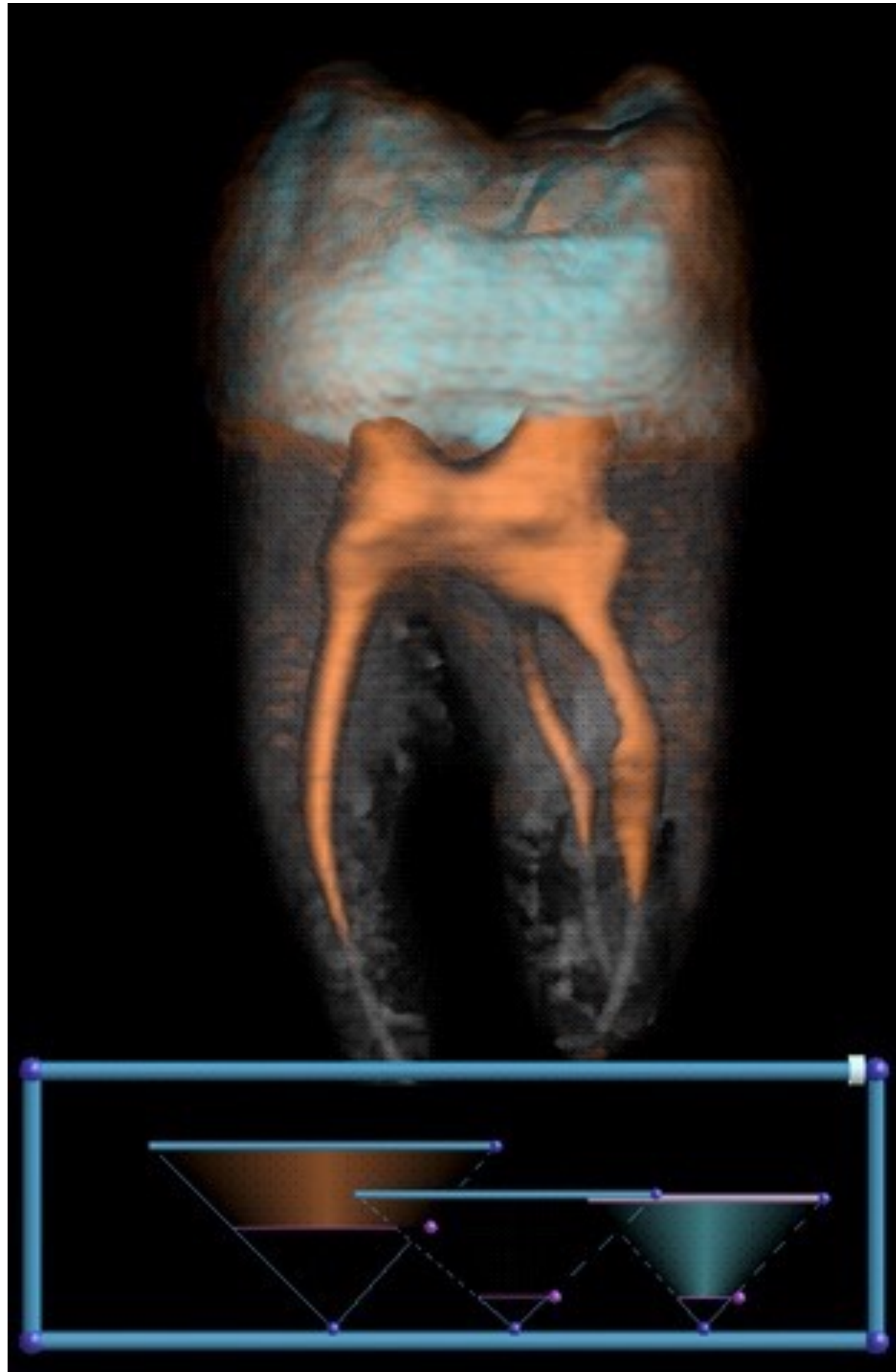
# Multidimensional Transfer Functions



[J. Kniss]



# Multidimensional Transfer Functions



[J. Kniss]